

*Note: 請將題號及答案標示清楚

1. (30%) Figure 1 shows a feedback control system with $G_p(s) = \frac{1}{ms + b}$, where $m=5$ and $b=2$.

- (1) (10%) Determine the characteristic equation of this system and the controller gains of K_p , K_i , K_v such that the poles are located at $-0.5 \pm j0.5, -10$.
- (2) (10%) Determine the steady-state error with $R=0$ when the disturbance is
 - (a) a unit step, (b) ramp function $d(t)=3t$, (c) parabolic function $d(t)=t^2/2$.
- (3) (10%) Neglect the real pole. Assume $D=0$ and $R(t)$ is a unit step. Sketch the step response of this system.

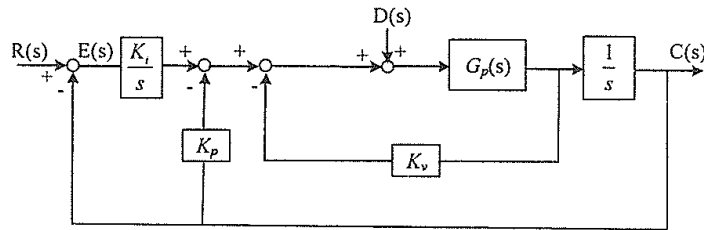


Figure 1

2. (20%) Consider the system in Figure 2.

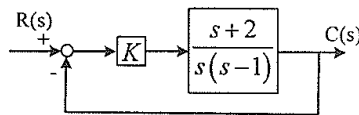


Figure 2

- (1) (10%) Draw the root-locus as K varies from 0 to infinity. Find asymptote, the value of K where the root loci cross the imaginary axis, the values of K at the break-away point, break-in point, and the closed-loop poles for these K values.
- (2) (10%) When the system is stable, find the range of K for the system is underdamped. If the design specification requires the damping ratio for the dominant closed-loop poles is equal to 0.707, determine the value of K and the closed-loop poles for this K value.

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3. (20%) Refer to Figure 3 with $G(s) = \frac{s+1}{s-9}$ and $C(s) = \frac{9}{s}$,
- (1) (5%) Sketch the Bode plots of $L(s) = G(s)C(s)$.
 - (2) (5%) Sketch the Nyquist plot of $L(s) = G(s)C(s)$.
 - (3) (5%) Calculate the gain margin of the system.
 - (4) (5%) Calculate the phase margin of the system.

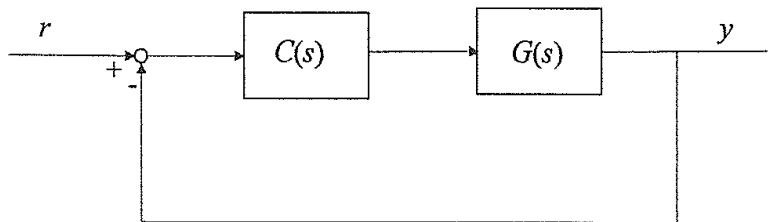


Figure 3

4. (30%) Consider Figure 3 with $G(s) = \frac{10(s+1)}{s(s-9)}$,
- (1) (5%) Suppose $C(s) = K \in R$, sketch the root-loci of the closed-loop system as $K : 0 \rightarrow \infty$. Mark the important values of K on the plot.
 - (2) (5%) Find the range of K that can maintain system stability by the Nyquist Criterion.
 - (3) (5%) Find the frequency ω_1 , where $|G(j\omega_1)|=1$.
 - (4) (5%) Design a first-order controller $C(s)$ to assign all closed-loop poles at $s = -2$.
 - (5) (10%) Design a controller $C(s) = \frac{k(s+z)}{s+p}$ such that the system has a phase margin of greater than 45° and a bandwidth of less than 20 rad/sec.

試題隨卷繳回