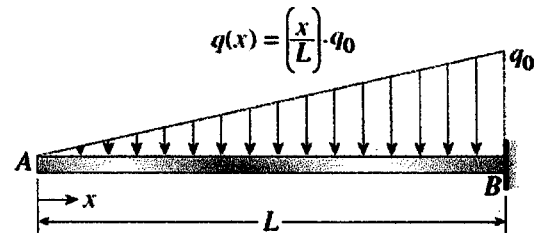


Question 1 (25%)

A cantilever beam AB is subjected to a linearly increasing load:

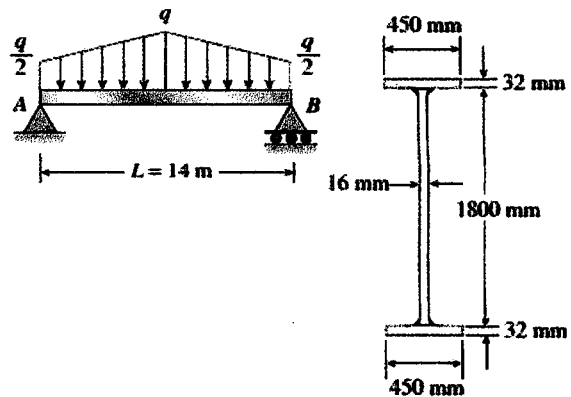
- (a) Derive the equations of shear force $V(x)$ and bending moment $M(x)$ of this beam. (10%)
- (b) Plot shear force and bending moment diagrams of this beam and clearly mark the maximum and minimum values and their locations. (15%)



Question 2 (25%)

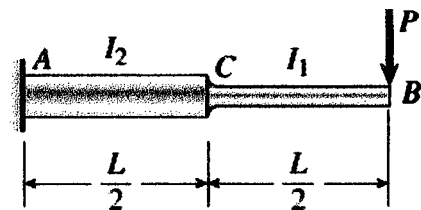
A bridge girder AB on a simple span of length $L = 14$ m supports a distributed load of maximum intensity q at mid-span and minimum intensity $q/2$ at supports A and B that includes the weight of the girder. The girder is made of a steel beam of wide-flange shape.

- (a) Calculate the load q based upon the yield stress of the steel material $\sigma_y = 110$ MPa. (10%)
- (b) Calculate the load q based upon the shear strength of the steel material $\tau = 50$ MPa. (10%)
- (c) Design the maximum allowable load that this beam can bear based on the load q determined in (a) and (b). Assume the factor of safety is $FS = 2$. (5%)



Question 3 (25%)

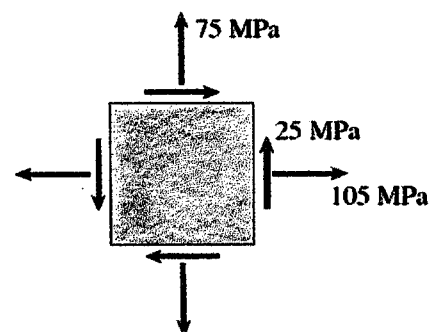
The cantilever beam ACB has moments of inertia I_2 and I_1 in parts AC and CB , respectively. Determine the deflection δ_B at the free end due to the load P .



Question 4 (25%)

An element is under plane stress conditions subjected to $\sigma_x = 105$ MPa, $\sigma_y = 75$ MPa, and $\tau_{xy} = 25$ MPa.

- (a) Discuss what is the purpose of doing stress transformation. (5%)
- (b) Determine the principal stresses and the orientation of the principal planes. Show them on a sketch of a properly oriented element. (10%)
- (c) Determine the maximum shear stresses and the orientation of the planes corresponding to the maximum shear stresses. Show them on a sketch of a properly oriented element. (10%)



試題隨卷繳回