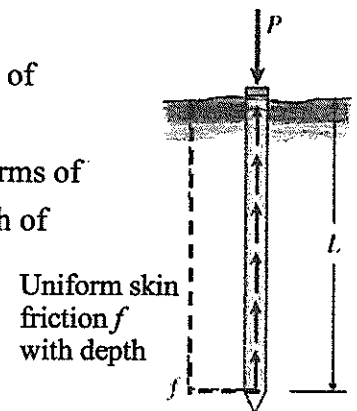


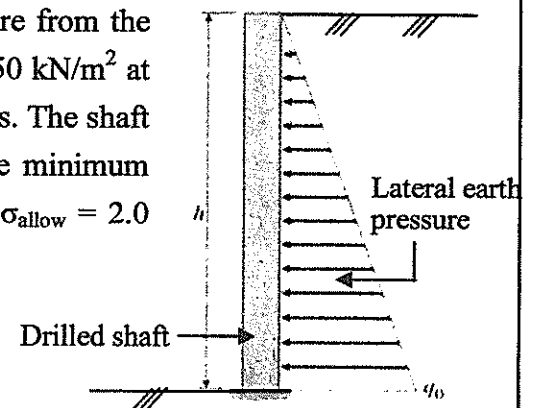
Question 1 (25%)

A steel pile supports a load P entirely by friction along its sides. The friction force f per unit length of pile is assumed to be uniformly distributed over the surface of the pile. The pile has length L , cross sectional area A , and modulus of elasticity E . Derive a formula for the shortening δ of the pile in terms of P , L , E , and A . Draw a diagram showing how the compressive stress σ_c varies throughout the length of the pile.



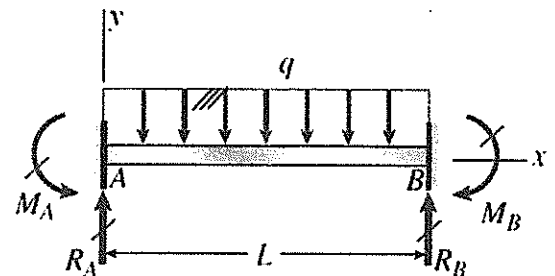
Question 2 (25%)

A series of drilled shafts is constructed as a tangent pile wall to resist lateral earth pressure from the retained soil. The lateral earth pressure is linearly distributed with depth and reaches $q_0 = 50 \text{ kN/m}^2$ at the bottom. Because the shaft is embedded into the ground so that it acts as cantilever beams. The shaft has a circular cross-section with the diameter of d and height $h = 5.0 \text{ m}$. Determine the minimum required dimension d of the shafts if the allowable bending stress of the pile material is $\sigma_{\text{allow}} = 2.0 \text{ MPa}$.



Question 3 (25%)

A fixed-end beam AB of length L supports a uniform load of intensity q . Beginning with the second-order differential equation of the deflection curve (the bending-moment equation), obtain the reactions R_A , M_A , R_B , and M_B . Determine the slope and deflection of the beam at $x = L/2$. Construct the shear-force and bending-moment diagrams, labeling all critical ordinates.



Question 4 (25%)

An underground soil element is subjected to principal stresses σ_x , σ_y , and σ_z . The σ_z is the effective soil overburden pressure and σ_x and σ_y are the effective soil lateral earth pressure ($\sigma_x = \sigma_y$). Use three-dimensional Hooke's law and assume soil is under at-rest conditions (no deformation in x and y direction), prove the following equation:

$$K_o = \frac{\nu}{1-\nu}$$

where K_o is at-rest earth pressure coefficient and ν is Poisson's ratio.

