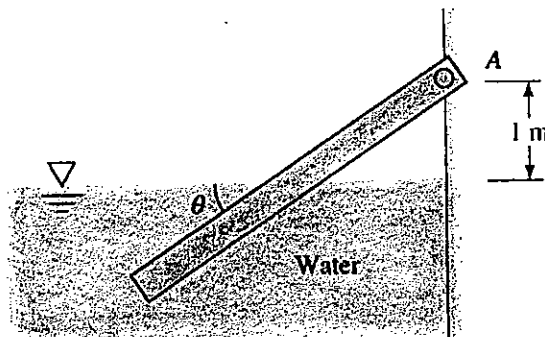
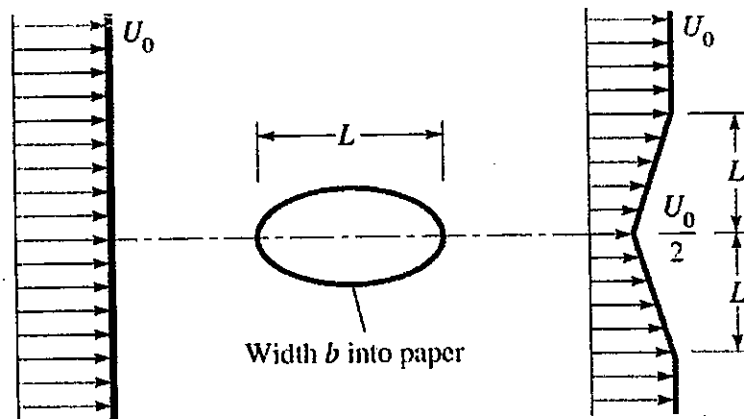


1. (25%) A uniform wooden beam (specific gravity = 0.65) is 10 cm by 10 cm by 3 m and is hinged at A, as in the following figure. At what angle will the beam float in the 20°C water ( $\rho = 998 \text{ kg/m}^3$ )?

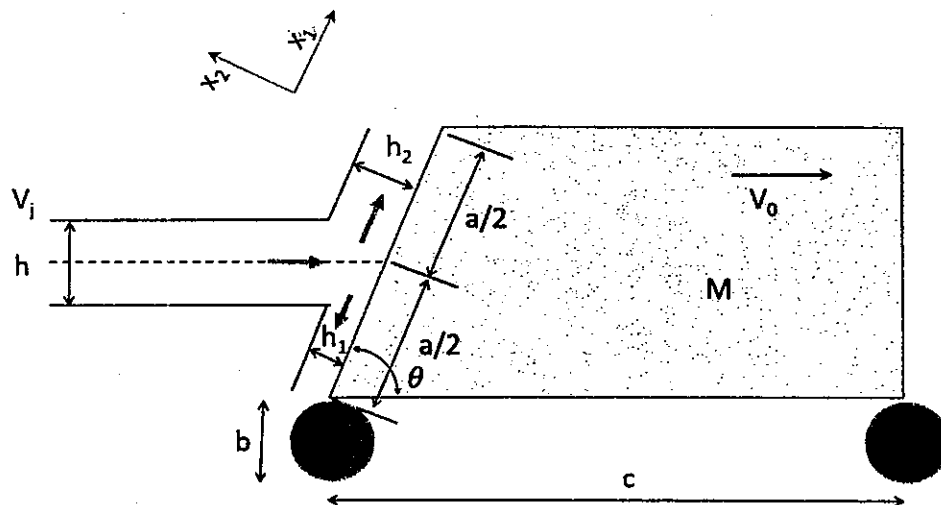


2. (25%) When immersed in a uniform stream, a thick elliptical cylinder creates a broad downstream wake, as idealized in the following figure. The pressure at the upstream and downstream sections are approximately equal, and the fluid is water at 20°C ( $\rho = 998 \text{ kg/m}^3$ ). If  $U_0 = 4 \text{ m/s}$  and  $L = 80 \text{ cm}$ , estimate the drag force (N) on the cylinder per unit width into the paper. Also compute the dimensionless drag coefficient  $C_D = 2F / (\rho U_0^2 b L)$ .



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3. (25%) A steady, incompressible, frictionless (inviscid), two dimensional jet of water with density  $\rho$ , width  $h$ , velocity  $V_j$ , impinges on a cart, moving at a constant velocity  $V_0$ , as shown below. The gravity is to be neglected.
- (a.) (10%) Determine  $h_1$  and  $h_2$ , which are, respectively, the water-level heights at the lower and upper parts after the jet impinges the cart.
- (b.) (5%) Determine the friction acting on the cart.
- (c.) (10%) Determine the reaction (including force and torque) of each wheel.



4. (25%) The flow pattern in bearing lubrication is illustrated by a steady two-dimensional flow as shown below. A viscous oil with density  $\rho$  and viscosity  $\mu$  is forced into the thin gap  $h(x)$  between a fixed slipper block and a wall moving at velocity  $U$ .
- (a.) (5%) Is there a velocity component ( $v$ ) in the  $y$ -direction? If yes, under what condition can it be neglected?
- (b.) (5%) What are the boundary conditions for the  $x$ -component velocity  $u$  within the gap?
- (c.) (15%) If the condition in (a.) applies ( $v = 0$  or to be neglected), neglecting gravity, find  $u = u(y)$  (in terms of  $h(x)$ ,  $h_1$ ,  $h_2$ ,  $\mu$ ,  $U$ , and  $y$ ).

