

- For van der Waals equation,
  - Please write van der Waals equation (3 %)
  - Please find the critical point ( $T_c, p_c, v_c$ ) (9 %)
  - Assume  $T_r = T/T_c, p_r = P/p_c, v_r = v/v_c$ , please show that van der Waals equation can be written as  $(p_r + \frac{3}{v_r^2})(v_r - \frac{1}{3}) = \frac{8}{3}T_r$  (8 %)
- For ideal gas is under a reversible and adiabatic process, please prove  $pV^\gamma = \text{constant}$ . ( $\gamma = C_p/C_v$ ) (10 %)
- At 27 °C, one mole ideal gas is under reversible expansion from 1 liter to 1.5 liter isothermally. Calculate the work generated during this process. (10 %) ( $\ln 1.5 = 0.4055$ )
- One liter of a 0.1 M solution of a substance A is added to two liters of a 0.05 M solution of a substance B. Assume ideal behavior of mixing, please calculate the entropy of mixing. (10 %) ( $\ln 3 = 1.0986; \ln 1.5 = 0.4055$ )
- Please derive following equations (F: Helmholtz free energy, G: Gibbs free energy)
  - $d\left(\frac{F}{T}\right) = -\frac{U}{T^2}dT - \frac{P}{T}dV$  (5 %)      b)  $d\left(\frac{G}{T}\right) = -\frac{H}{T^2}dT - \frac{V}{T}dP$  (5 %)
  - $U = -T^2\left(\frac{\partial}{\partial T}\left(\frac{F}{T}\right)\right)_v$  (5 %)      d)  $H = -T^2\left(\frac{\partial}{\partial T}\left(\frac{G}{T}\right)\right)_p$  (5 %)
- One mole ideal gas is under the process (Carnot cycle) as shown in the figure.
  - Please calculate the efficiency,  $\eta$ , of this cycle. (5 %)
  - Please calculate the maximum work can be produced in one cycle. (10 %) ( $\ln 2 = 0.69315$ )
- In a reaction taking place in the body at 37°C, the change in enthalpy was  $-125 \text{ kJ mol}^{-1}$  and the change in entropy was  $-126 \text{ J K}^{-1} \text{ mol}^{-1}$ .
  - Calculate the change in Gibbs energy. (5 %)
  - Calculate the total change in entropy of the system and the surroundings. (5 %)
- The enthalpy of the phase transition from graphite to diamond which under 100 kbar occurs at 2000 K is  $1.9 \text{ kJ mol}^{-1}$ . Calculate the entropy of transition at that temperature. (5%)

