

1. (a) What is linear time-variant (LTI) system? (5%)
 (b) Please provide an operational definition for LTI system such that a real system can be tested. (10%)
2. (a) Please draw the block-diagram of a general feedback control system. (Please mark all the functional blocks and variables clearly.) (15%)
 (b) With the block diagram, please explain why such a feedback configuration can achieve our control goal of regulation normally? (Hint: what is regulation? how can it be achieved with the feedback configuration?) (10%)
3. Suppose a dynamical system is modeled by a set of dynamical equations in the following:

$$\begin{cases} (M + m)\ddot{x} + b\dot{x} - ml\ddot{\theta} \cos \theta + ml\dot{\theta}^2 \sin \theta = F \\ (I + ml^2)\ddot{\theta} - mgl \sin \theta = ml\ddot{x} \cos \theta \end{cases}$$

with $M=0.8, m=0.2, l=1.0, b=2, I=0.8, g=10.0$. Also assume the operating point of the system is at $\theta=0$ and $\dot{\theta}^2 \sim 0$.

- (a) Please derive the transfer function model $G(s)$ of the dynamical system. (10%)
- (b) Suppose that the dynamical system $G(s)$ is put into a closed-loop system as in Figure 1, please determine the range of k_1 ($C(s)=k_1$) such that the closed-loop system to be stable. (10%)
- (c) Please draw the root locus of the closed-loop system in Figure 1. (10%)
4. Given a Bode Plot for a dynamic system G as in Figure 2, please answer the following questions:
 - (a) Is the dynamic system G stable? (5%)
 - (b) What is Phase Margin (PM)? How is it related to the stability of a system as in Figure 1? (5%)
 - (c) What properties of G can you read from the Bode Plot in Figure 2? (10%)
 - (d) How should we design a compensator if PM is to be greater than 45 degrees and the steady-state error is to be smaller than 0.01? (10%)

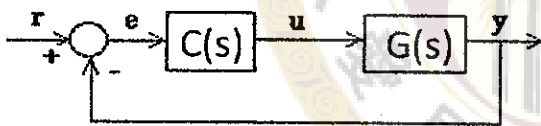


Figure 1 A feedback control system

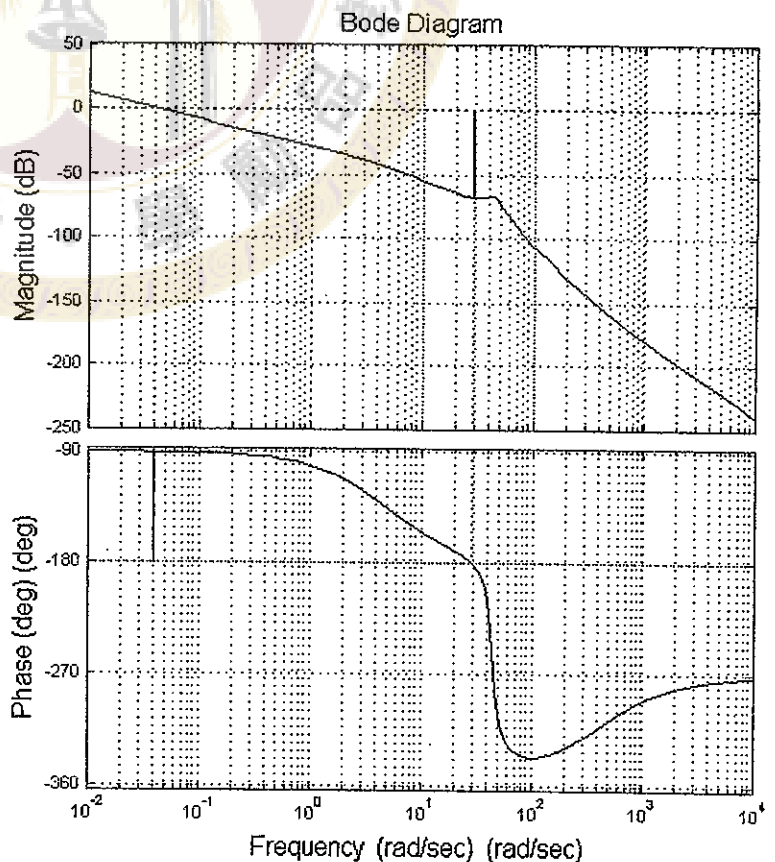


Figure 2 Bode plot on the right