

1. Explain the following terms:

(a) Ideal fluid

(5 points)

(b) Newtonian fluid

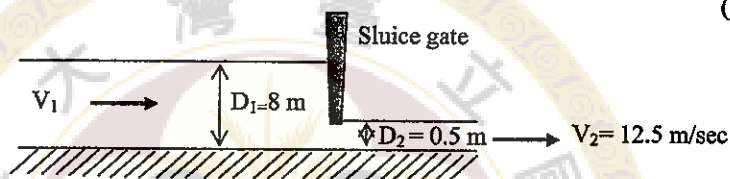
(5 points)

2. Write the Navier-Stokes equation describing an incompressible viscous flow, and explain the meaning of each term in the equation.

(10 points)

3. Water flows under a sluice gate on a horizontal, rectangular channel. Flow is frictionless and uniform. The depth of the upstream is 8 m. Water discharges with a flow velocity of 12.5 m/sec under the sluice gate in a 0.5 m deep flow. Use the Bernoulli equation to determine the velocity of the upstream.

(15 points)



4. Water flows in a rectangular channel on a bed slope of 0.0005. The flow rate is 200 m<sup>3</sup>/sec and  $n$  is 0.022. Determine the required dimensions of the best hydraulic cross section (The normal depth should be one-half the width of the channel bottom).

(15 points)

5. A Newtonian fluid with viscosity  $\mu$  flows in one dimension with horizontal ( $x$  direction) velocity  $u$  which varies vertically ( $y$  direction).

(a) Write an expression (equation) describing the shear stress  $\tau$  exerted in the  $x$ -direction on a fluid surface at  $y$  is.

(b) Also give the units of  $\mu$ ,  $u$  and  $\tau$ .

(10 points)

6. A Newtonian fluid of density  $\rho$  and viscosity  $\mu$  flows downward ( $z$ -direction) in cylindrical pipe of radius  $R$ . At vertical upstream position  $z = 0$  and downstream position  $z = L$ , the static pressures are  $p_0$  and  $p_L$ , respectively. The gradient of laminar flow velocity ( $u_z$ ) in  $z$ -direction with respect to radius direction  $r$  can be describe as

$$du_z/dr = -[(p_0 + \rho gL) - p_L]/(2\mu L)$$

(a) Obtain the velocity distribution of  $u_z$  at various  $r$ .

(b) Calculate the maximum velocity  $u_{z,max}$ .

(c) Compute the average velocity  $u_{z,avg}$ .

(d) Calculate the volume rate of flow  $Q$ .

(e) Compute the force of the fluid on the wetted surface of the pipe  $F_z$ .

(f) Define a proper Reynolds number of the pipe flow system.

(30 points)

7. A sphere solid with radius  $R$  and density  $\rho_s$  is allowed to fall from rest in a viscous fluid with density  $\rho$  and viscosity  $\mu$  and accelerate until it reaches a constant (terminal) velocity  $u_t$ .

(a) Make a force balance on the sphere solid if the drag force  $F_d$  can be describe by the Stokes's law with

$$F_d = 6\pi\mu R u_t.$$

(b) Compute the  $\mu$ .

(10 points)

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