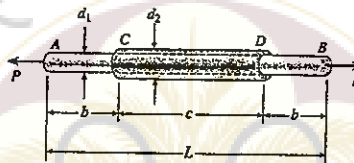


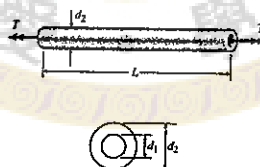
(20%) 1. A plastic rod  $AB$  of length  $L = 0.5$  m has a diameter  $d_1 = 30$  mm. A plastic sleeve  $CD$  of length  $c = 0.3$  m and outer diameter  $d_2 = 45$  mm is securely bonded to the rod so that no slippage can occur between the rod and the sleeve. The rod is made of an acrylic with modulus of elasticity  $E_1 = 3.1$  GPa and the sleeve is made of a polyamide with  $E_2 = 2.5$  GPa.

- (a) Calculate the elongation  $d$  of the rod when it is pulled by axial forces  $P = 12$  kN. (8%)
- (b) If the sleeve is extended for the full length of the rod, what is the elongation? (6%)
- (c) If the sleeve is removed, what is the elongation? (6%)



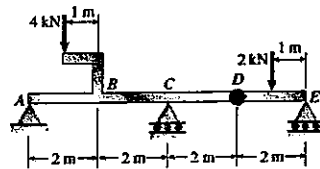
(15%) 2. A hollow aluminum shaft has outside diameter  $d_2 = 100$  mm and inside diameter  $d_1 = 50$  mm. When twisted by torques  $T$ , the shaft has an angle of twist per unit distance equal to  $2^\circ/\text{m}$ . The shear modulus of elasticity of the aluminum is  $G = 27.5$  GPa.

- (a) Determine the maximum tensile stress  $\sigma_{\max}$  in the shaft. (8%)
- (b) Determine the magnitude of the applied torques  $T$ . (7%)

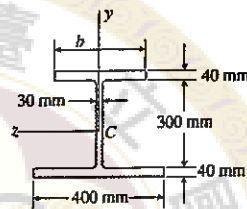


(15%) 3. The compound beam  $ABCDE$  consists of two beams ( $AD$  and  $DE$ ) joined by a hinged connection at  $D$ . The hinge can transmit a shear force but not a bending moment. The loads on the beam consist of a 4-kN force at the end of a bracket attached at point  $B$  and a 2-kN force at the midpoint of beam  $DE$ . Draw the shear-force and bending-moment diagrams for this compound beam.

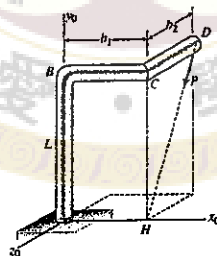
見背面



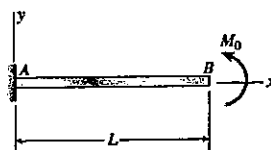
(15%) 4. A beam having a cross section in the form of an unsymmetric wide-flange shape is subjected to a negative bending moment acting about the  $z$  axis. Determine the width  $b$  of the top flange in order that the stresses at the top and bottom of the beam will be in the ratio 4:3, respectively.



(20%) 5. A bracket  $ABCD$  having a hollow circular cross section consists of a vertical arm  $AB$  ( $L = 1.85$  m), a horizontal arm  $BC$  parallel to the  $x_0$  axis, and a horizontal arm  $CD$  parallel to the  $z_0$  axis. The arms  $BC$  and  $CD$  have lengths  $b_1 = 1.1$  m and  $b_2 = 0.67$  m, respectively. The outer and inner diameters of the bracket are  $d_2 = 190$  mm and  $d_1 = 170$  mm. An inclined load  $P = 10$  kN acts at point  $D$  along line  $DH$ . Determine the maximum tensile, compressive, and shear stresses in the vertical arm.



(15%) 6. Derive the equation of the deflection curve for a cantilever beam  $AB$  when a couple  $M_0$  acts counterclockwise at the free end. Also, determine the deflection  $\delta_B$  and slope  $\theta_B$  at the free end. (The beam described above has constant flexural rigidity  $EI$  and the origin of coordinate is at the left-hand end of the beam.)



試題隨卷繳回