

※ 注意：選擇題請於試卷之「選擇題作答區」依序作答。

第一部分：社會統計 (50分)

(一) 單選題(每題 三分，請將題號及答案標示清楚寫在答案紙上，沒有題號者不允許分)。

1. _____. Which of the following statement is **incorrect**?
 - A. A distribution has zero skewness if it is symmetrical about its mean.
 - B. For a symmetrical distribution, the mean, median, and mode are equal.
 - C. A distribution is positively skewed (skew to the right) if the right tail is longer.
 - D. A distribution is negatively skewed (skew to the left) if mean > median > mode.
2. _____. A nation faces a rate of inflation of 2% in one year, 5% in the second year, and 12.5% in the third year. Find the geometric mean of the inflation rates.
 - A. 5%
 - B. 6.5%
 - C. 11.18%
 - D. 6.45%
3. _____. Consider the regression equation: $y = \beta_0 + \beta_1x + \beta_2x^2$, which of the following statements regarding this equation is **incorrect**:
 - A. When $\beta_1 > 0$ and $\beta_2 < 0$, the equation implies a diminishing marginal effect of x on y .
 - B. The statement that x has a diminishing marginal effect on y is the same as saying that y decreases as x increases.
 - C. The slope of the regression is approximately $\beta_1 + 2\beta_2x$
 - D. The maximum of the function occurs at the point $x^* = \beta_1 / (-2\beta_2)$
4. _____. Which of the following statements about the expected value is **NOT** correct:
 - A. if $\{a_1, a_2, \dots, a_n\}$ are constants and X_i are random variables, then $E(\sum_{i=1}^n a_i X_i) = \sum_{i=1}^n a_i E(X_i)$
 - B. If $E(X) = \sum_{i=1}^n x_i f(x_i)$, then $E[\log(X)] = \sum_{i=1}^n \log(x_i) f(x_i)$
 - C. If X_1, \dots, X_n are n random variables such that each expectation $E(X_i)$ exists, then $E(X_1 \cdot X_2 \cdot X_3 \dots X_n) = E(X_1)E(X_2) \dots E(X_n)$
 - D. $E(X^2)$ will not necessarily equal to $[E(X)]^2$
5. _____. For a random variable X , let $u = E(X)$, then
 - A. $\text{Var}(X) \equiv [E(X - u)]^2$
 - B. For any constant a and b , $\text{Var}(aX + b) = a^2 \text{Var}(X) + b$
 - C. $\text{Var}(X) = E(X^2) - E(X)^2$
 - D. $\text{Var}(X) = \sum_{i=1}^n (x_i) f(x_i) - u^2$
 - E. $\text{Var}(\sum_{i=1}^n a_i X_i) = \sum_{i=1}^n a_i^2 \text{Var}(X_i)$
6. _____. Let $E(X) = u_x$, $E(Y) = u_y$, which of the following statements regarding the covariance between X and Y are **incorrect**?
 - A. $\text{Cov}(X, Y) = E(XY) - u_x u_y$
 - B. $\text{Cov}(X, Y) = E[(X - u_x)Y]$
 - C. If $\text{Cov}(X, Y) = 0$, then X and Y are independent.
 - D. $\text{Cov}(X, Y) = E[(X - u_x)(Y - u_y)]$

7. _____. Which of the following properties regarding conditional expectations and conditional variance is **incorrect**?
- If X and Y are independent, the $E(Y|X) = E(Y)$
 - $E[E(Y|X)] \neq E(Y)$
 - If X and Y are independent, then $\text{Var}(Y|X) = \text{Var}(Y)$
 - If $E(Y|X) = E(Y)$, then every function of X is uncorrelated with Y
8. _____. Given a very simple random sample $\{Y_1, Y_2, \dots, Y_n\}$ drawn from a population distribution with population mean $E(Y) = \mu$ and variance $\text{Var}(Y) = \sigma^2$, which of the following is **incorrect**:
- $E(Y_1) = \mu$
 - $\text{Var}(Y_2) = \sigma^2$
 - $\text{Var}(\bar{Y}) = \sigma^2 / \sqrt{n}$
 - $E[\frac{1}{n-1} \sum_{i=1}^n (Y_i - \bar{Y})^2] = \sigma^2$
9. _____. Consider the simple regression equation: $y = \beta_0 + \beta_1 x + e$, which of the following statements is **correct**:
- if the dependent variable is multiplied by a constant c , then the new OLS intercept is also multiplied by c .
 - if the independent variable is divided by some nonzero constant c , the new OLS slope coefficient is divided by c .
 - if the dependent variable is multiplied by a constant c , then the new OLS slope estimate will not change.
 - all of the above.
10. _____. Suppose the true regression model is:
 $\text{Wage} = \beta_0 + \beta_1(\text{education}) + \beta_2(\text{ability}) + e$, but we do not have information about "ability". We estimate the following model instead: $\text{Wage} = \tilde{\beta}_0 + \tilde{\beta}_1(\text{education}) + \varepsilon$
 If "education" has a positive effect on wage and "education" and "ability" is positively correlated, then
- $\beta_1 > \tilde{\beta}_1$
 - $\beta_1 = \tilde{\beta}_1$
 - $\beta_1 < \tilde{\beta}_1$
 - It cannot be decided

(二) 簡答題，每題五分：

- 在OLS的簡單迴歸模型中，要具備那些條件或在那些假設(assumptions)之下，樣本迴歸模型所估計的斜率(slope)，才會是母體斜率的不偏估計式(unbiased estimator)? 請寫出迴歸分析的基本假定。
- 簡單解釋下列名詞(1) type I error (2) type II error (3) the power of a significant test。
- 想要比較白人(White)、非裔(African American)、西裔(Hispanic)等美國三大種族之間的平均收入是否有差別，可以用什麼方法來進行統計分析?為什麼不可以用三組t-test檢定來進行?若要在控制教育年數及年齡之下比較各組的差異，則要如何進行比較合適?
- 簡單說明測量上的reliability與validity的意義。

第二部分 研究方法(50 分)

駱明慶分析 1997 - 2000 年台大人學生的學籍資料，發現相較於全國平均的 0.89%，3.06%的台北市人口和 6.10%的大安區人口會成為台大學生，台東縣的比例則只有 0.19%。另外，台大法/社科學院的學生中，42%的父親和 27%的母親為大學畢業生，父親或母親為公教人員的比例高達 42%，均遠高於大學生和一般人口的比例。

1. 請基於以上研究資料，請你具體說明 (25%)
 - (1) 相關與因果有何不同？
 - (2) 上述發現可能衍生哪些因果假設？
 - (3) 可以透過怎樣的設計來檢驗這些假設？

2. 從以上資料，請你發展出一個質性的研究，請具體說明 (25%)
 - (1) 你的研究問題
 - (2) 如何收集資料、選擇個案
 - (3) 具體討論質性與量化研究對於研究這個命題的優缺點

試題隨卷繳回