

每題 20 分 共五題 請依題號次序作答

- I. Consider an unsteady, two-dimensional, incompressible velocity field with

$$\vec{V} = (x+1)\vec{i} + (-y+3+5\sin t)\vec{j}$$

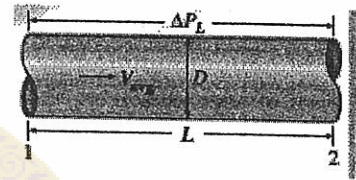
- (1) Consider a fluid particle initially ($t = 0$) at position $(x, y) = (0, 0)$, what will be the location of this particle at time $t = 2\pi$.
 (2) Find the equation of streamline which pass through $(x, y) = (0, 0)$ at time $t = 2\pi$.

- II. In fully developed laminar flow in a circular pipe, the velocity profile is given by: $u(r) = 2V(1 - \frac{r^2}{R^2})$; where V is the average velocity. Show that the volume flow rate, Vol , in the pipe can be expressed by the so

called Poiseuille's equation: $Vol = A \frac{\Delta P \pi D^4}{\mu L}$; where L is the pipe

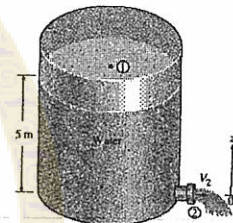
length, D is the pipe diameter, ΔP is the total pressure drop.

Determine the value of the constant A in the Poiseuille's equation.



- III. (1) A large tank open to the atmosphere is filled with water to a height of 5 m from the outlet tap. A tap near the bottom of the tank is now opened, and water flows out from the smooth and rounded outlet. Determine the water velocity at the outlet. ($g = 9.8 \text{ m/s}^2$).

- (2) If the diameters of the tank and the outlet are D_1 (1.0 m) and D_2 (0.03 m) respectively, determine how long it will take for the water level in the tank to drop to 2.5 m from the bottom.



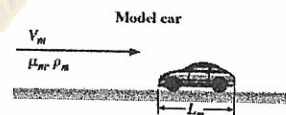
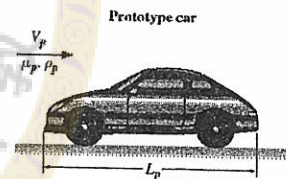
- IV. If the drag force F_D of a sport car moving with constant velocity V in air is a function of air density ρ , viscosity μ and its size, (characteristic length), L , i.e. $F_D = f(V, L, \rho, \mu)$. The drag force of a new sport car is to be predicted at a speed of 90 km/hr. Automotive engineers build a 1/5 scale model of the car to be tested in a water tunnel.

- (1) Determine how fast the model car should be run in the water tunnel in order to achieve dynamic similarity between the model and the prototype.

- (2) If the drag force at this water tunnel testing speed is measured to be 20 N, and the length of the prototype is $L_p = 3.8 \text{ m}$. what is the drag force of the prototype?

$$\rho_{air} = 1.2 \text{ kg/m}^3; \mu_{air} = 1.85 \times 10^{-5} \text{ kg/(m}\cdot\text{s)}$$

$$\rho_{water} = 1.0 \times 10^3 \text{ kg/m}^3; \mu_{water} = 1.0 \times 10^{-3} \text{ kg/(m}\cdot\text{s)}$$



- V. Consider a fluid particle moving along with a streamline. The velocity of the particle along a streamline is given as $V = V(s, t)$, where s is the distance along the streamline and t is time. Derive the Bernoulli's Equation along a streamline for a steady incompressible flow. (Please write down all the details of your derivation)

