

1.

- (a) Discuss the existence condition of Laplace Transform. (5%)
- (b) Discuss the existence condition of Fourier Transform. (5%)
- (c) According to (a) and (b), please discuss their relation with the pole positions in the  $s$ -plane and explain if they are stable? (10%)

2.

A feedback control system is shown in Fig.1. Please find the values of the control parameters  $k_1$  and  $k_2$  to achieve the following conditions for the closed-loop step response. (20%)

- (i) peak time  $T_p = 1$  sec
- (ii) settling time  $T_s = 2$  sec

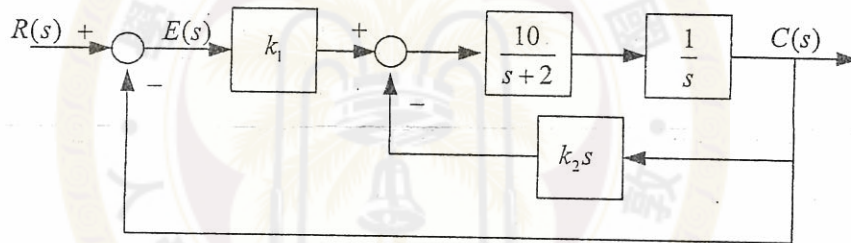


Fig. 1

3.

A control system has three closed-loop poles, including two conjugated imaginary poles and one real pole, as shown in Fig. 2.

- (a) Please find the value of  $K$  according to the Routh stability criterion. (10%)
- (b) Please find the values of the three poles in accordance with (a). (10%)

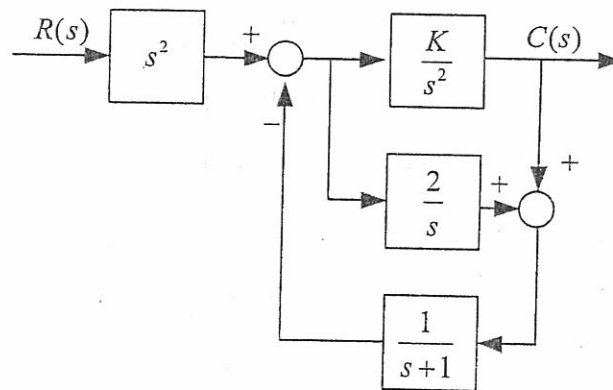


Fig. 2

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4.

A position control system is shown in Fig.3, which open-loop transfer function is

$$G(s) = \frac{10}{s(s+2)}$$

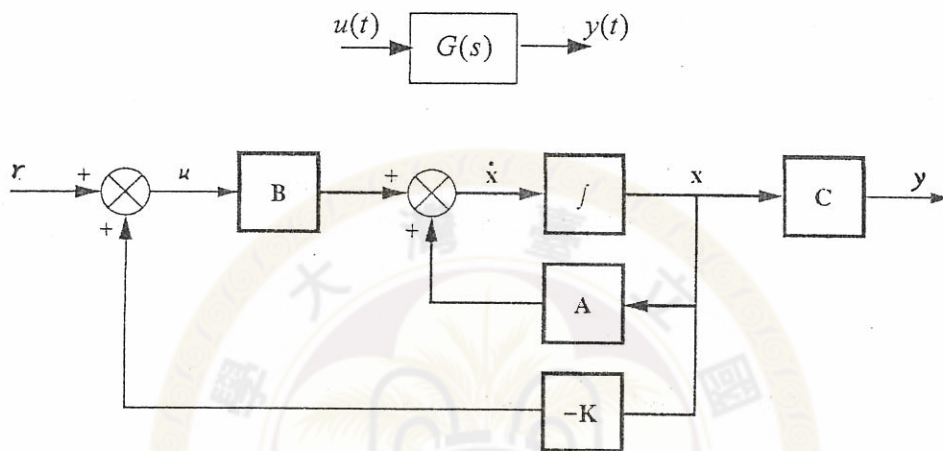


Fig. 3

- Derive the state space equation using the state variables  $x_1 = y$  and  $x_2 = dy/dt$ . (5%)
- Design a state feedback controller  $K$  for  $u = -KX$  to match the closed-loop conditions:  $\xi = 1/\sqrt{2}$ ;  $\omega_n = 2\sqrt{2}$ . (8%)
- If an unit step function is given as reference input  $r$ , please solve the steady state error. (7%)

5.

An unity feedback control system has the open-loop transfer function as

$$G(s) = \frac{\omega_n^2}{s(s + 2\xi\omega_n)}$$

- Please find the closed-loop transfer function  $T(s)$ . (5%)
- Please find the relation between the phase margin (PM) and the damping ratio  $\xi$ . (8%)
- Please find the relation between  $|T(j\omega_c)|$  and PM, where  $\omega_c$  is the crossover frequency of the open-loop system using the Nyquist plot. (7%)

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