

- Please find the **mean** and **variance** of the following p.d.f.
(a) $f(x) = 1/5, x = 5, 10, 15, 20, 25$ (5%); (b) $f(x) = \frac{1}{b-a}, a \leq x \leq b$ (10%);
(c) $f(x) = \frac{3!}{x!(3-x)!} \left(\frac{1}{4}\right)^x \left(\frac{3}{4}\right)^{3-x}, x = 0, 1, 2, 3$ (5%)
- Given three events $A_1, A_2,$ and A_3 such that $P(A_1) = 0.3, P(A_2) = 0.6, P(A_3) = 0.4;$
 $P(A_1 \cap A_2) = 0.2, P(A_1 \cap A_3) = 0.1, P(A_2 \cap A_3) = 0.3;$ and $P(A_1 \cap A_2 \cap A_3) = 0.05.$
Please find (a) $P(A_1 \cup A_2 \cup A_3)$ and (b) $P(A_1' \cap A_2' \cap A_3')$ (10%)
- Let \bar{X} be the sample mean of a random sample of size 16 from $\mathcal{N}(2, 4),$ and let \bar{Y} be the sample mean of another random sample of size 4 from **the same parent population.**
(1) What are the distributions of \bar{X} and $\bar{Y},$ respectively? (5%)
(2) What is the distribution of $\bar{X} - \bar{Y}$ (5%)
(3) Please find the probability $P(\bar{X} - \bar{Y} > 0)$ (5%)
- Let $f(x)$ be the p.d.f. of a binomial distribution. Using the **binomial theorem,** please show that $\sum_{x=0}^n f(x) = 1.$ (25%)
- An animal ecologist suggests three methods to prevent squirrels from damaging *Cryptomeria* plantations. To determine the effectiveness of the three methods, a small experiment was conducted with 9 replications for each treatment (method). The **Treatment Total** of each method is listed below. Mean square error (**MSE**) of the experiment is 60. Please (1) state an appropriate model and its assumptions, (2) state the null and alternative hypotheses, and (3) construct a complete ANOVA table based on the given information and state your conclusions. Let the type I error rate of the test be 0.05. Please use **Table 1** to find the critical value for the test. Assuming all the regular assumptions hold. (30%)

	Method		
	I	II	III
Treatment Total	243	324	189

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Table 1. The entries are the probabilities $P(X \geq x) = 0.05$, where X follows an F -distribution with numerator degrees of freedom n , and denominator degrees of freedom m

		Numerator degrees of freedom n					
		1	2	3	4	5	6
denominator degrees of freedom m	20	4.35	3.49	3.10	2.87	2.71	2.60
	21	4.32	3.47	3.07	2.84	2.68	2.57
	22	4.30	3.44	3.05	2.82	2.66	2.55
	23	4.38	3.42	3.03	2.80	2.64	2.53
	24	4.26	3.40	3.01	2.78	2.62	2.51
	25	4.24	3.39	2.99	2.76	2.60	2.49
	26	4.23	3.37	2.98	2.74	2.59	2.47
	27	4.21	3.35	2.96	2.73	2.57	2.46