

\*Note: 請清楚標示答案

1. (25%) Considering the following state-space model  $G: \begin{cases} \dot{x} = \begin{bmatrix} -1 & -1 \\ 3 & 2 \end{bmatrix} x + \begin{bmatrix} 1 \\ 1 \end{bmatrix} u \\ y = \begin{bmatrix} 1 & 1 \end{bmatrix} x \end{cases}$

- (a) (5%) Find the corresponding transfer function  $G(s)$ .  
 (b) (5%) Refer to the feedback structure of Figure 1 and suppose the controller  $K$  is constant, find the range of  $K$  such that the closed-loop system is stable.  
 (c) (5%) Find the suitable value of  $K$  such that the damping-ratio of the closed-loop system is  $\sqrt{3}/2 = 0.866$ .  
 (d) (5%) Derive the output response  $y(t)$  to a unit step input  $r(t) = \begin{cases} 1, & \text{for } t \geq 0 \\ 0, & \text{for } t < 0 \end{cases}$  with the  $K$  from (3).  
 (e) (5%) According to (4), find the settling time (defined as variations less than 2%) of the response.

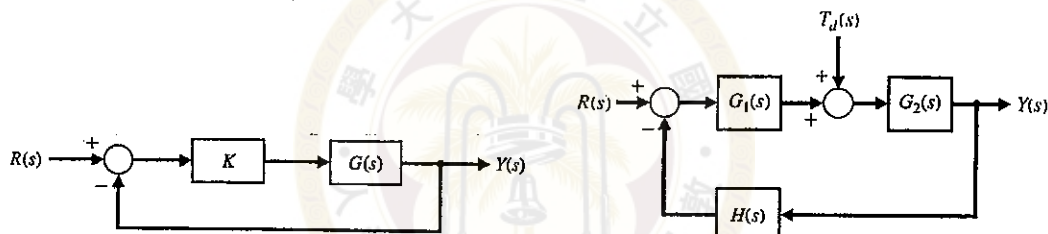


Figure 1

Figure 2

2. (25%) Considering the feedback system of Figure 2 with  $G_2(s) = \frac{1}{s^2 + 2s + 5}$  and  $H(s) = 1$ , a first-order controller is required in order to arbitrarily assign the closed-loop pole.
- (a) (5%) Find a first-order controller  $G_1(s) = K_1(s) = \frac{b_1s + b_0}{s + a_0}$ , such that the characteristic equation of the closed-loop system is  $\Delta(s) = (s + 2)(s^2 + 4s + 5)$ .  
 (b) (5%) Find the sensitivity of the closed-loop transfer function  $T_{R \rightarrow Y}$  to the variations of  $a_0$ , using the parameters obtained from (1).  
 (c) (5%) Find the steady-state error of the system due to a unit step input  $R(s)$ , using the first-order controller  $K_1(s)$  from (1).  
 (d) (5%) In order to eliminate the steady-state errors, an integral is normally applied to the controller, i.e.  $G_1(s) = K_2(s) = \frac{b_2s^2 + b_1s + b_0}{s^2 + a_1s}$ . Find the second-order controller  $K_2(s)$  such that the characteristic equation of the closed-loop system is  $\Delta(s) = (s + 2)^2(s^2 + 4s + 5)$ .  
 (e) (5%) Using the controller  $K_2(s)$  from (4), find the transfer functions  $T_{T_d \rightarrow Y}$ , and the steady-state error of the output due to a unit step disturbance  $T_d$ .

見背面

3. (30%) A feedback control system shown in Figure 3 is to be designed to satisfy the following specifications: (1) steady state error for a ramp input  $\leq 35\%$  of input slope; (2) percentage overshoot for a step input  $\leq 4.4\%$ ; (3) settling time to within 2% for a step input  $\leq 3$  sec; (4) peak time for a step input  $\leq 2$  sec.

- (a) (5%) If  $G_c = K_I$  and  $H_1 = 0$ , explain why all specifications can not be met simultaneously.  
 (b) (8%) If  $H_1 = 0$ , can the system with phase-lead or phase-lag controller  $G_c$  satisfies all the specifications? Explain your reasons.  
 (c) (10%) If  $G_c = K_I$  and  $H_1 = K_2s$ , find appropriate parameters  $K_I$  and  $K_2$  of the system so all the specifications are met (using root locus technique).  
 (d) (7%) Following (c), sketch Bode diagram of the closed-loop system.

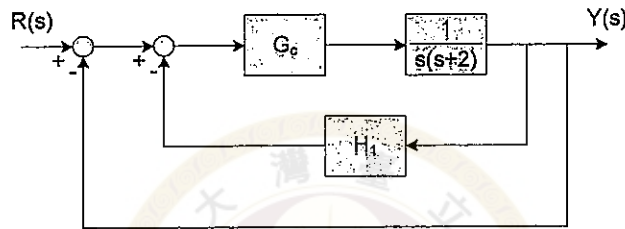


Figure 3

4. (10%) Sketch Nyquist diagram of the system whose bode diagram is shown in Figure 4.

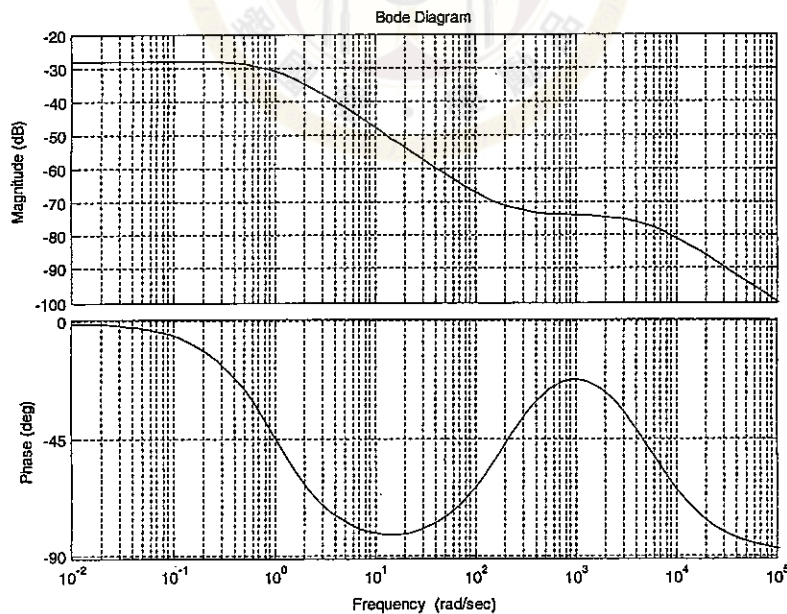


Figure 4

5. (10%) Analytically derive bandwidth  $\omega_B$  of the closed-loop system with forward transfer function

$$G = \frac{\omega_n^2}{s(s + 2\zeta\omega_n)} \text{ and negative unity feedback.}$$

試題隨卷繳回