

1. (25%) Find the capacitance  $C$  of two concentric spherical metal shells, with radii  $R$  and  $2R$ .

2. (25%) Find the magnetic field  $\mathbf{B}$  at a distance  $z$  above the center of a circular loop of radius  $R$ , which carries a steady current  $I$ .

3. (a) (10%) Can the vector field  $\vec{E} = (yz - 2x)\hat{i} + xz\hat{j} + xy\hat{k}$  possibly be an electrostatic field? Please verify it.

(b) (15%) What is the charge distribution in this electric field  $\vec{E} = (yz - 2x)\hat{i} + xz\hat{j} + xy\hat{k}$ ?

4. (a) (10%) Please explain why we can use  $\vec{E} = -\nabla V$  in electrostatics?  $\vec{E}$ : electric field,  $V$ : potential.

(b) (15%) A (physical) electric dipole consists of two equal and opposite charges  $+q$  and  $-q$ , which are separated by a distance  $d$ . The approximate potential at points far from the dipole is

$$V(\vec{r}) = \frac{1}{4\pi\epsilon_0} \frac{qd \cos \theta}{r^2}$$

Please derive the electric field  $\vec{E}$ .

Hint:  $\vec{E} = -\nabla V = -\frac{\partial V}{\partial r}\hat{r} - \frac{1}{r}\frac{\partial V}{\partial \theta}\hat{\theta} - \frac{1}{r \sin \theta}\frac{\partial V}{\partial \phi}\hat{\phi}$

