題號: 98

國立臺灣大學 103 學年度碩士班招生考試試題

科目:應用數學(B)

節次: 2 共) 頁之第 人

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Please answer each of the following questions showing all of your work and discussing your reasoning so that I can follow what you've done and give partial credit.

- 1. Find the derivative of z = f(x, y) where $z = \sin x + \ln(xy) + y^4$ (10%)
- 2. Find the integration of $\int \frac{x^2 dx}{ax+b}$, where a and b are constant variables. (10%)
- 3. (a) Calculate the dot product of the following two vectors and determine whether or not the two vectors are orthogonal:

$$A = 8i - 3j + 2k, B = -8i - 3j + k$$
 (10%)

(b) Calculate the cross product of the following two vectors $(A \times B)$:

$$A = 2i - 3j + 4k$$

$$B = -3i + 2j$$
(10%)

4. Find the general solution of the following ordinary differential equations:

(a)
$$y' + xy = xy^2$$
 (10%)

(b)
$$y'-2y=-8x^2$$
 (10%)

5. Find the general solution of the following differential equation for positive and negative value of n.

$$\frac{d^2z}{dt^2} = -n^2z \quad (10\%)$$

6. Find the (a) determinant, (b) eigenvalues and (c) the corresponding eigenvectors

$$\begin{array}{ccc}
 & 3 & 0 & 0 \\
 & 1 & -2 & -8 \\
 & 0 & -5 & 1
\end{array}$$
(30%)