

1. (a) (8%) What is Poynting's theorem?
- (b) (8%) What is Helmholtz theorem?
- (c) (5%) What is the intrinsic impedance of a material medium for the electromagnetic wave?
- (d) (5%) What is the loss tangent of a material medium for the electromagnetic wave?
- (e) (10%) Write down the boundary conditions of electromagnetic waves propagating through the interface between two arbitrary media?

2. (14%) Charge is distributed with uniform density ρ_0 C/m³ in the spherical region $r < a$. Find the electric displacement field \vec{D} everywhere.

3. (14%) Consider two electric fields given by

$$\vec{E}_1 = (C\vec{a}_x + C\vec{a}_y + \vec{a}_z)\cos(10^9t - 10z) \text{ V/m}$$

$$\vec{E}_2 = (\vec{a}_x + C\vec{a}_y - 2\vec{a}_z)\sin(10^9t - 10z) \text{ V/m}$$

- (a) Find the polarization of $\vec{E}_1 + \vec{E}_2$ for $C=2$.
 - (b) Find the value of C for which $\vec{E}_1 + \vec{E}_2$ is circularly polarized.
4. (16%) Region 1 ($z < 0$) is free space, whereas region 2 ($z > 0$) is a perfect dielectric medium characterized by $\epsilon = 4\epsilon_0$, $\mu = \mu_0$. For a uniform plane wave having the electric field

$$\vec{E} = E_0 \cos(3 \times 10^8 t - z)\vec{a}_x$$

normal incident on the interface $z=0$ from region 1, obtain the expression for the reflected and the transmitted electric fields.

5. (20%) The electric field of a uniform plane wave propagating in a perfect dielectric medium having $\mu = \mu_0$ is given by

$$\vec{E} = 10 \cos(3 \times 10^7 t + 0.2x)\vec{a}_z \text{ V/m}$$

- (a) Find the phase velocity.
- (b) Find the permittivity of the medium.
- (c) Find the associated magnetic field \vec{H} .
- (b) Find the time-average Poynting vector.