

總分 100 分

1. Stability is the most important system specification. Please explain the following problems about stability:

(a) Please explain the natural response definition of stability. (5%)

(b) Please explain the BIBO definition of stability. (5%)

(c) In the unity feedback system of Fig.1 with  $G(s) = \frac{1}{4s^2(s^2 + 1)}$ , please use the

Routh-Hurwitz criterion to discuss the locations of the the closed-loop poles in the  $s$ -plane. (10%)

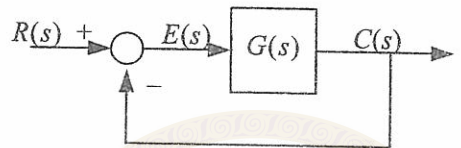


Fig.1

2.

Please clarify the following important problems of automatic control:

(a) Please explain the following terms using a differential equation:

(i) linear and nonlinear (4%)

(ii) time-invariant and time-variant (4%)

(iii) causal and noncausal (4%)

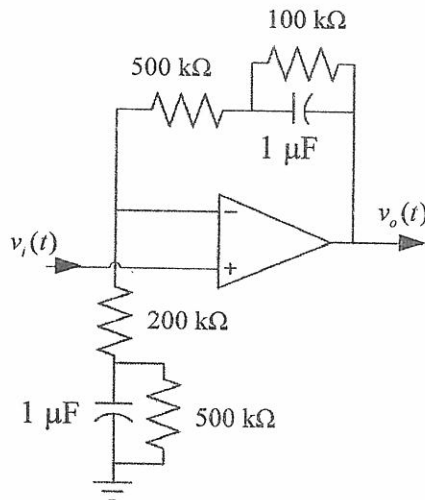
(b) What kind of systems is discussed in automation control. (4%)

(c) Please explain the difference of the initial conditions between transfer function and state equation. (4%)

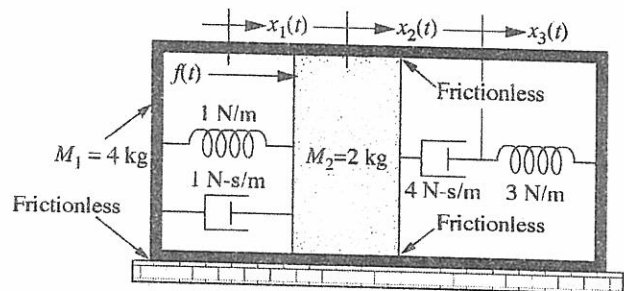
3. Find the transfer function of the following systems:

(a)  $G(s) = V_o(s)/V_i(s)$  (10%)

(b)  $G(s) = X_3(s)/F(s)$  (10%)



(a)



(b)

Fig.2

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4. A control system is shown in Fig.3.

where  $D(s) = \frac{s+a}{s+8}$  and  $G(s) = \frac{10}{s(s+1)}$

(a) Sketch the root locus plot. (10%)

(b) Determine the value of  $a$  such that the damping ratio of the dominant poles is  $\zeta = 0.5$ .

(10%)

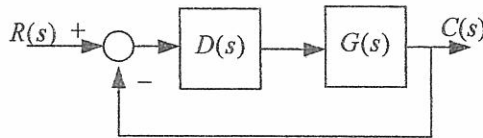


Fig.3

5. A unity-feedback system is shown in Fig.3 with  $G(s) = \frac{1}{s(s+2)}$

(a) Please design a phase-lead compensator  $D(s) = \beta \frac{1+\alpha Ts}{1+Ts}$  to make the loop transfer function  $D(s)K(s)$  satisfy the following conditions: (i) velocity constant=10; (ii) phase margin= $60^\circ$ ; (iii) gain margin  $\geq 12$  dB. (15%)

(b) If a phase-lag compensator is designed for the same system and conditions as (a), please explain the differences between the phase-lead compensated and the phase-lag compensated systems. (5%)