

1. **Quantum theory of atoms (22%)**

(a) (4%) What is the electron configuration of Ge? (for example $1s^2 2s^2 2p^5$ for F atoms).

(b) (4%) For an electron in the valence band (outmost shell) of Ge crystals, what are the possible sets of quantum numbers? Neglect the hybridization of s and p orbitals. Treat them as discrete orbitals. Note that for each set, you MUST write down its four quantum numbers (n, l, m_l, m_s) .

(c) (14%) Considering spin-orbit coupling for an electron of the outmost shell in Ge by treating a Ge atom like hydrogen atom, please calculate the following parameters: radius ($r = n^2 a_0$, $a_0 = 0.529 \text{ \AA}$), electron velocity ($m = 0.1m_0$), frequency, magnetic field ($B = \frac{\mu_0 f e}{2r}$, $\mu_0 = 4\pi \times 10^{-7}$), and the energy difference ($\Delta E = \frac{e\hbar B}{m}$) of the splitting states in terms of eV and its equivalent temperature.

2. **Quantum Mechanics (28%)**

A particle of mass m is in a delta potential quantum well of

$$U(x) = -A\delta(x)$$

(a) (14%) If $E < 0$, it is called "bound states" case. Wave function can be expressed as $\sqrt{B}e^{-Bx}$. Find B and the associated energy level.

(Hint: 1. $\psi(x)$ is continuous and 2. $\frac{d\psi(x)}{dx}$ is continuous except at $x = 0$).

(b) (14%) If $E > 0$, it is called "scattering states" case. See Fig. 1 for scattering details. Assume an incident electron from the left (i.e. $G = 0$), what are the reflection coefficient ($R = \frac{|B|^2}{|A|^2}$), transmission

coefficient ($T = \frac{|F|^2}{|A|^2}$)? Please show that $R + T = 1$. Express R and

T in terms of m, A, \hbar, E ,

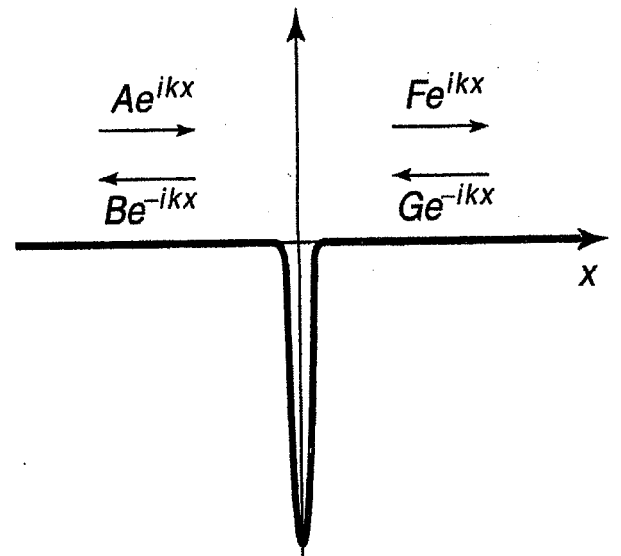


Fig. 1 An electron incident on a delta potential.

3. **Semiconductor physics and devices (50%)**

For a n-MOSFET (Fig. 2), if N_D in the n-type source/drain region is $5 \times 10^{19} \text{ cm}^{-3}$ and N_A in the p-type substrate is 10^{17} cm^{-3} . $N_C = 2.8 \times 10^{19} \text{ cm}^{-3}$ and $N_V = 1 \times 10^{19} \text{ cm}^{-3}$.

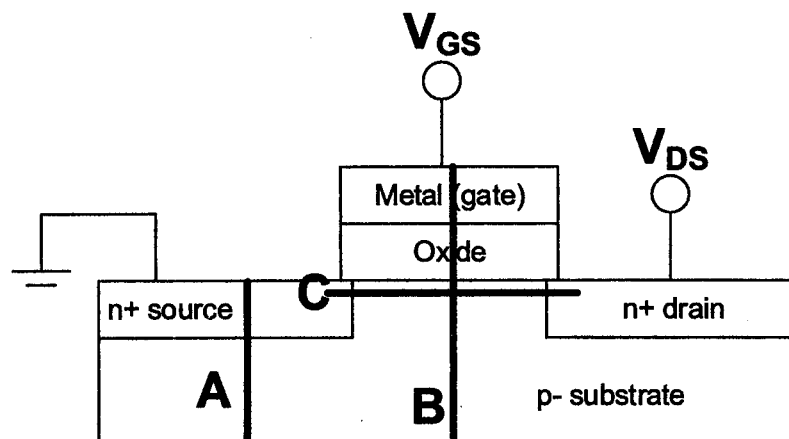


Fig. 2 A n-type Si MOSFET device

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- (a) (4%) Calculate $E_F - E_V$ in the p-type Si substrate.
- (b) (6%) Please draw the band diagram along line A by labeling all energy levels (and its relative positions in the source and substrate regions). You can assume $E_F \sim E_C$ in the n+ source region.
- (c) (10%) Please qualitatively draw the band diagram along line B. Assume $V_{GS} = 2$ V, $V_{FB} = 0$ V, and the system is in strong inversion. Label the energy levels of E_{FM} (Fermi level in metal), E_C , E_i , E_{FS} (Fermi level in semiconductor), and E_V . Note that you also need to mark the energy differences between (i) E_{FS} and E_{FM} , (ii) E_{FS} and E_V in the bulk p-Si, and (iii) E_{FS} and E_C at the oxide/p-Si interface.
- (d) (10%) Please qualitatively draw the band diagram along line C (in the Si region and right at the oxide/Si interface). Following (c) by assuming the system is in strong inversion and $V_{DS} = 2$ V. Label the energy levels of E_C , and E_V , and Fermi levels in the source (E_{FS}), drain (E_{FD}), and channel (E_{FC}). You need to mark the energy differences between (i) E_{FS} and E_{FD} , (ii) E_{FC} and E_C at the oxide/p-Si interface.
- (e) (10%) Considering the following parameters: work function of metal gate, substrate doping level, and oxide thickness. Please describe how we could vary the above three parameters to reduce the threshold voltage.
- (f) (10%) Considering the following parameters: gate length, oxide capacitance, and mobility. Please describe how we could adjust the above three parameters to enhance the device performance in MOSFETs (i.e. higher current density).

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