

Problem 1 (20%)

Determine the radix r for the following equations.

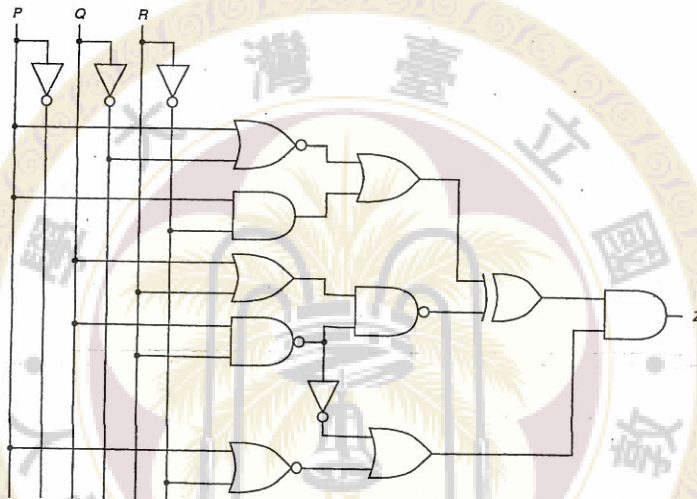
(% is the remainder operator, e.g., $9 \% 4 = 1$.)

a. $21_r \times 13_r - 24_r = 245_r$

b. $(25_r \times 41_r) \% 28_r = 21_r$

Problem 2 (20%)

Simplify the following circuit; use as few gates (AND, OR, and NOT) as possible.



Problem 3 (20%)

A Moore sequential circuit M has one input X and one output Z . M behaves as follows.

1. When $Z = 0$ and the input sequence 010 occurs, Z becomes 1 and remains 1 until the sequence 101 occurs in which case Z returns to 0.
2. When $Z = 1$ and the input sequence 101 occurs, Z becomes 0 and remains 0 until the sequence 010 occurs in which case Z returns to 1.
3. At the beginning, Z equals 0.

The following is an example.

X	110100100110011011011100010101011110...
Z	0000000111111111000000000111000000...

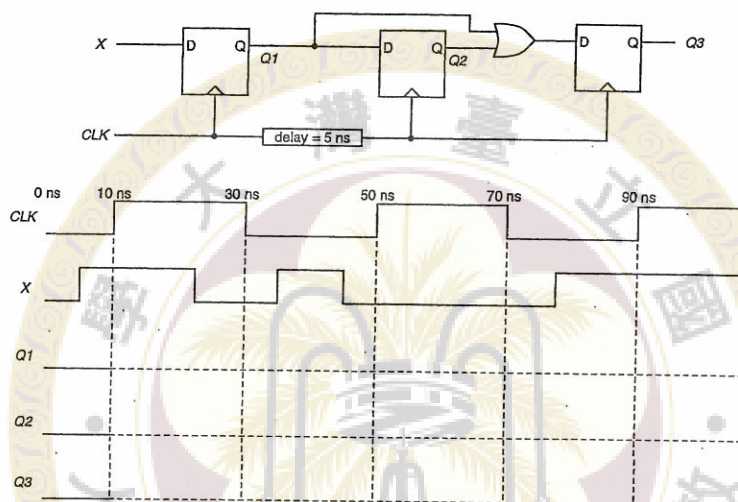
Derive and simplify the state graph of M .

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Problem 4 (20%)

Complete the timing diagram for the given circuit. Assume that

1. the D flip-flop has a 2-ns propagation delay and zero setup/hold time,
2. the OR gate has a 1-ns propagation delay,
3. the delay element has a 5-ns propagation delay, and
4. the initial values of Q_1 , Q_2 , and Q_3 are 0.



Problem 5 (20%)

1. What output sequence ($Q_1Q_2Q_3$) does the counter below generate (assuming that the initial counter state is not all 0's)?
2. Modify the counter so that it repeatedly generates a sequence of all eight outputs, i.e., including $Q_1Q_2Q_3 = 000$, without affecting the order of the original sequence.

