

請於答案卷上依序作答，並註明題號，須列計算過程，否則不予計分，共12題，共100分，答案請四捨五入至小數第三位。

1. Ellen is taking a typing lesson and her assignment is to type a 10-page report in one hour. The number of typing errors she makes per page has a Poisson distribution with mean of $\lambda=2$.

(a) (5 points) What is the probability that Ellen does not make any typing error in one randomly selected page?

(b) (5 points) What is the probability that Ellen makes 4 typing errors total in two pages?

(c) (5 points) Randomly select 4 pages from the report and inspect them. Find the probability that 2 of those pages have no error.

(d) (5 points) Suppose you inspect Ellen's report from the first page, one page at a time. What is the probability that the fourth page is the first one that has no error?

2. Two car loan officers, George and Mary, try to compare who is working harder. They looked at the time spent on communications with buyers during one month. Assume that the individual times are normally distributed with unknown parameters. George worked with 12 customers. He spent in average 45 minutes per customer, with the standard deviation of 6 minutes. Mary worked with 16 customers, spent in average 40 minutes, with the standard deviation of 4 minutes.

George believes that the population variances should be equal, and Mary objected saying that population variances are entirely unknown.

(a) (3 points) What standard error will be assessed to the difference between two sample means if you take George's view that the population variances are the same?

(b) (3 points) How many degrees of freedom will you set sharing Mary's view that population variances are unknown?

(c) (5 points) Whose assumption about the population variances is more likely to be true, George's or Mary's? (significance level=10%)

(d) (9 points) Does George have enough evidence that the average time he spent with each customer is more than Mary (significance level =10%)? Please specify the test statistic values and the critical value.

3. Mr. Chen is a wine manager for a restaurant. He is trying to determine which of three wine-growing regions in California have the best wines. He randomly selects 5 bottles of red wine and 5 bottles of white wine from each region, and has them rated by a

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professional wine taster. The tables below give the partial computer output of a 2-way ANOVA, along with the cell means (the average ratings for the 5 bottles of wine).

Dependent Variable: Rating

Source	Sum of Squares	df	Mean Square
Wine	2.315	1	0.382
Region	240.556	2	120.278
Wine*Region	117.963	2	58.981
Error	145.556	??	??

Cell means of average rating

	Region 1	Region 2	Region 3
Red wine	23.333	23.000	13.000
White wine	19.333	20.333	18.000

- (a) (2 points) Compute the Mean Square of Error.
 (b) (3 points) Does there appear to be a main effect of Wine, a main effect of Region, and/or an interaction between Wine and Region ($\alpha=.05$)? Why or why not?
 (c) (5 points) Based on the tables given above and your answers to (b), explain the taste testing results in plain language to Mr. Chen, the wine manager.

4. (5 points) Let x be a random variable with the following probability density function:

$$f(x) = \binom{6}{x} p^x (1-p)^{6-x}, x = 0, 1, 2, 3, 4, 5, 6$$

One randomly takes 100 samples from the population and obtains the following results:

x	0	1	2	3	4	5	6
frequency	15	8	20	29	7	11	10

Find the maximum likelihood estimator of $p(x < 2)$.

5. (5 points) A psychologist wants to know how many hours the average baby sleeps per day. He takes a random sample of 6 individuals and records each baby how many hours he or she slept the previous day. He obtains the following results: 13.2, 16.1, 17.8, 16.9, 20.1, 17.7 hours. Find a 95% confidence interval for the mean number of hours of sleep.

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6. (5 points) Consider a random variable X follows a uniform distribution over the interval $(0, y)$ with y unknown. Find $a\%$ confidence interval of y with sample size 1.

7. (8 points) Suppose a random sample of 10 (x_1, \dots, x_{10}) is taken from a normal distribution with the mean μ and the variance σ^2 unknown. One student tests the following hypothesis: $H_0: \mu = 0$; $H_1: \mu \neq 0$ and concludes that the null hypothesis is rejected only if the test statistic V is such that $V < a$ or $V > b$ where $p(V < a) = 0.025$ and $p(V > b) = 0.05$. Find $a+b$ and whether the null hypothesis should be rejected given that $\sum_{i=1}^{10} x_i = -3.4$ and $\sum_{i=1}^{10} x_i^2 = 43.4$.

8. (7 points) One statistician uses the least squares method to find the regression of Y on X : $\hat{Y}_t = -3.8 + 5.3X_t$ and the relationship between X_t and e_t is as follows ($t=1, 2, \dots, 6$):

X_t	0	2	4	6	8	10
e_t	3.1	-2.8	5.2	-6.7	0.8	??

Find e_6 and Y_6 as well as the coefficient of correlation.

9. (5 points) A and B play 100 rounds of table tennis game. Then how many rounds that A should win so that one can conclude A is really better than B under $\alpha=0.05$.

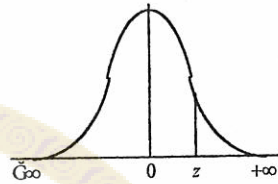
10. (5 points) Let $f(x, y) = 1/24$ be the joint probability density function of X and Y where $0 \leq x \leq 6$, and $0 \leq y \leq 12$. Test whether X and Y are independent.

11. (5 points) Let $f(x, y)$ be the joint probability density function of X and Y such that $f(x, y) = k$ for $0 < x < y < 4$ and $f(x, y) = 0$ otherwise. Find k .

12. (5 points) One researcher wants to do a survey regarding one type of birds in a bird sanctuary. Assume the total number of this type of birds is N . Three months ago, the researcher caught a of them, and put a mark on each bird and release. This time, the researcher catches b birds of the same type and m of them have the mark. Find the maximum likelihood estimator of N .

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NORMAL DISTRIBUTION TABLE



	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	.9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	.9995
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998

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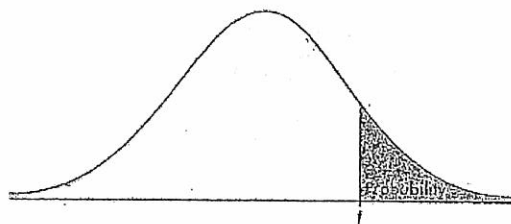


TABLE B: *t*-DISTRIBUTION CRITICAL VALUES

df	Tail probability <i>p</i>											
	.25	.20	.15	.10	.05	.025	.02	.01	.005	.0025	.001	.0005
1	1.000	1.376	1.963	3.078	6.314	12.71	15.89	31.82	63.66	127.5	318.3	636.6
2	.816	1.061	1.386	1.886	2.920	4.303	4.849	6.965	9.925	14.09	22.33	31.60
3	.765	.978	1.250	1.638	2.353	3.182	3.482	4.541	5.841	7.453	10.21	12.92
4	.741	.941	1.190	1.533	2.132	2.776	2.999	3.747	4.604	5.598	7.173	8.610
5	.727	.920	1.156	1.476	2.015	2.571	2.757	3.365	4.032	4.773	5.893	6.869
6	.718	.906	1.134	1.440	1.943	2.447	2.612	3.143	3.707	4.317	5.208	5.959
7	.711	.896	1.119	1.415	1.895	2.365	2.517	2.998	3.499	4.029	4.785	5.408
8	.706	.889	1.108	1.397	1.860	2.306	2.449	2.896	3.355	3.833	4.501	5.041
9	.703	.883	1.100	1.383	1.833	2.262	2.398	2.821	3.250	3.690	4.297	4.781
10	.700	.879	1.093	1.372	1.812	2.228	2.359	2.764	3.169	3.581	4.144	4.587
11	.697	.876	1.088	1.363	1.796	2.201	2.328	2.718	3.106	3.497	4.025	4.437
12	.695	.873	1.083	1.356	1.782	2.179	2.303	2.681	3.055	3.428	3.930	4.318
13	.694	.870	1.079	1.350	1.771	2.160	2.282	2.650	3.022	3.372	3.852	4.221
14	.692	.868	1.076	1.345	1.761	2.145	2.264	2.624	2.977	3.326	3.787	4.140
15	.691	.866	1.074	1.341	1.753	2.131	2.249	2.602	2.947	3.286	3.733	4.073
16	.690	.865	1.071	1.337	1.746	2.120	2.235	2.583	2.921	3.252	3.686	4.015
17	.689	.863	1.069	1.333	1.740	2.110	2.224	2.567	2.898	3.222	3.646	3.965
18	.688	.862	1.067	1.330	1.734	2.101	2.214	2.552	2.878	3.197	3.611	3.922
19	.688	.861	1.066	1.328	1.729	2.093	2.205	2.539	2.861	3.174	3.579	3.883
20	.687	.860	1.064	1.325	1.725	2.086	2.197	2.528	2.845	3.153	3.552	3.850
21	.686	.859	1.063	1.323	1.721	2.080	2.189	2.518	2.831	3.135	3.527	3.819
22	.686	.858	1.061	1.321	1.717	2.074	2.183	2.508	2.819	3.119	3.505	3.792
23	.685	.858	1.060	1.319	1.714	2.069	2.177	2.500	2.807	3.104	3.485	3.768
24	.685	.857	1.059	1.318	1.711	2.064	2.172	2.492	2.797	3.091	3.467	3.745
25	.684	.856	1.058	1.316	1.708	2.060	2.167	2.485	2.787	3.078	3.450	3.725
26	.684	.856	1.058	1.315	1.706	2.056	2.162	2.479	2.779	3.067	3.435	3.707
27	.684	.855	1.057	1.314	1.703	2.052	2.158	2.473	2.771	3.057	3.421	3.690
28	.683	.855	1.056	1.313	1.701	2.048	2.154	2.467	2.763	3.047	3.408	3.674
29	.683	.854	1.055	1.311	1.699	2.045	2.150	2.462	2.756	3.038	3.396	3.659
30	.683	.854	1.055	1.310	1.697	2.042	2.147	2.457	2.750	3.030	3.385	3.646
40	.681	.851	1.050	1.303	1.684	2.021	2.123	2.423	2.704	2.971	3.307	3.551
50	.679	.849	1.047	1.299	1.676	2.009	2.109	2.403	2.678	2.937	3.261	3.496
60	.679	.848	1.045	1.296	1.671	2.000	2.099	2.390	2.660	2.915	3.232	3.460
80	.678	.846	1.043	1.292	1.664	1.990	2.088	2.374	2.639	2.887	3.195	3.416
100	.677	.845	1.042	1.290	1.660	1.984	2.081	2.364	2.626	2.871	3.174	3.390
1000	.675	.842	1.037	1.282	1.646	1.962	2.056	2.330	2.581	2.813	3.098	3.300
∞	.674	.841	1.036	1.282	1.645	1.960	2.054	2.326	2.576	2.807	3.091	3.291
	50%	60%	70%	80%	90%	95%	96%	98%	99%	99.5%	99.8%	99.9%
	Confidence level <i>C</i>											

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F - Distribution ($\alpha = 0.05$ in the Right Tail)

df ₂ \ df ₁		Numerator Degrees of Freedom								
		1	2	3	4	5	6	7	8	9
1	161.45	199.50	215.71	224.58	230.16	233.99	236.77	238.88	240.54	
2	18.513	19.000	19.164	19.247	19.296	19.330	19.353	19.371	19.385	
3	10.128	9.5521	9.2766	9.1172	9.0135	8.9406	8.8867	8.8452	8.8123	
4	7.7086	9.9443	6.5914	6.3882	6.2561	6.1631	6.0942	6.0410	6.9988	
5	6.6079	5.7861	5.4095	5.1922	5.0503	4.9503	4.8759	4.8183	4.7725	
6	5.9874	5.1433	4.7571	4.5337	4.3874	4.2839	4.2067	4.1468	4.0990	
7	5.5914	4.7374	4.3468	4.1203	3.9715	3.8660	3.7870	3.7257	3.6767	
8	5.3177	4.4590	4.0662	3.8379	3.6875	3.5806	3.5005	3.4381	3.3881	
9	5.1174	4.2565	3.8625	3.6331	3.4817	3.3738	3.2927	3.2296	3.1789	
10	4.9646	4.1028	3.7083	3.4780	3.3258	3.2172	3.1355	3.0717	3.0204	
11	4.8443	3.9823	3.5874	3.3567	3.2039	3.0946	3.0123	2.9480	2.8962	
12	4.7472	3.8853	3.4903	3.2592	3.1059	2.9961	2.9134	2.8486	2.7964	
13	4.6672	3.8056	3.4105	3.1791	3.0254	2.9153	2.8321	2.7669	2.7144	
14	4.6001	3.7389	3.3439	3.1122	2.9582	2.8477	2.7642	2.6987	2.6458	
15	4.5431	3.6823	3.2874	3.0556	2.9018	2.7905	2.7066	2.6408	2.5876	
16	4.4940	3.6337	3.2389	3.0069	2.8524	2.7413	2.6572	2.5911	2.5377	
17	4.4513	3.5915	3.1968	2.9647	2.8100	2.6987	2.6143	2.5480	2.4943	
18	4.4139	3.5546	3.1599	2.9277	2.7729	2.6613	2.5767	2.5102	2.4563	
19	4.3807	3.5219	3.1274	2.8951	2.7401	2.6283	2.5435	2.4768	2.4227	
20	4.3512	3.4928	3.0984	2.8661	2.7109	2.5990	2.5140	2.4471	2.3928	
21	4.3248	3.4668	3.0725	2.8401	2.6848	2.5727	2.4876	2.4205	2.3660	
22	4.3009	3.4434	3.0491	2.8167	2.6613	2.5491	2.4638	2.3965	2.3419	
23	4.2793	3.4221	3.0280	2.7955	2.6400	2.5277	2.4422	2.3748	2.3201	
24	4.2597	3.4028	3.0088	2.7763	2.6207	2.5082	2.4226	2.3551	2.3002	
25	4.2417	3.3852	2.9912	2.7587	2.6030	2.4904	2.4047	2.3371	2.2821	
26	4.2252	3.3690	2.9752	2.7426	2.5868	2.4741	2.3883	2.3205	2.2655	
27	4.2100	3.3541	2.9604	2.7278	2.5719	2.4591	2.3732	2.3053	2.2501	
28	4.1960	3.3404	2.9467	2.7141	2.5581	2.4453	2.3593	2.2913	2.2360	
29	4.1830	3.3277	2.9340	2.7014	2.5454	2.4324	2.3463	2.2783	2.2229	
30	4.1709	3.3158	2.9223	2.6896	2.5336	2.4205	2.3343	2.2662	2.2107	
40	4.0847	3.2317	2.8387	2.6060	2.4495	2.3359	2.2490	2.1802	2.1240	
60	4.0012	3.1504	2.7581	2.5252	2.3683	2.2541	2.1665	2.0970	2.0401	
120	3.9201	3.0718	2.6802	2.4472	2.2899	2.1750	2.0868	2.0164	1.9588	
∞	3.8415	2.9957	2.6049	2.3719	2.2141	2.0986	2.0096	1.9384	1.8799	

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