

Problem 1 (20%)

A dielectric material of permittivity ϵ sliding freely in a cylindrical capacitor experiences a mechanical force F_e of electric origin in the axial direction, as shown in Figure Problem-1.

(assuming the fringing effects at the edges negligible)

- (a) find the expression of electric field in the region of $a < r < b$
- (b) calculate the capacitance of such configuration in terms of the intrusion x
- (c) find the expression for F_e .

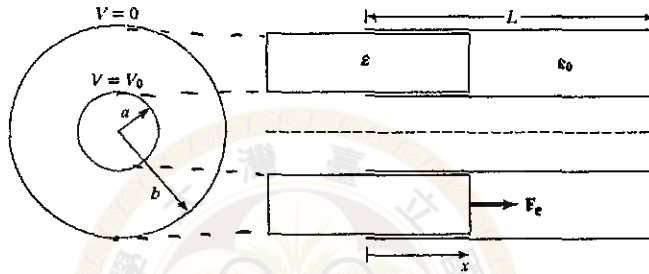


Figure Problem-1

Problem 2 (30%)

In Figure Problem-2, the region $z < 0$ is a perfect dielectric, whereas the region $z > 0$ is a perfect conductor. For an incident uniform plane wave having the electric field

$$\vec{E}_i = E_0 [\cos(\omega t - \beta z)\hat{x} - \sin(\omega t - \beta z)\hat{y}] \quad \text{where } \beta = \omega\sqrt{\mu\epsilon}$$

- (a) obtain the magnetic field of the incident wave (hint: using the wave impedance η)
- (b) determine the polarization sense of the incident wave (linear/circular? right/left handed?)
- (c) write down the boundary condition at $z=0$ and find the expressions for the electric and magnetic fields of the reflected waves
- (d) determine the polarization sense of the reflected wave (linear/circular? right/left handed?)
- (e) find the expressions of the total (incident + reflected) electric and magnetic fields; Are they standing waves?
- (f) find the induced current density on the surface of the perfect conductor
- (g) find the Poynting vector of the incident wave
- (h) find the Poynting vector of the total fields in the perfect dielectric

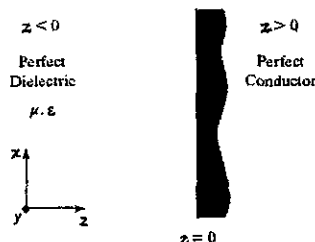


Figure Problem-2

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Problem 3. (30%)

- (a) Please define and explain the Brewster Angle. (5%)
- (b) What is the polarization of the reflected wave for an elliptically polarized wave incident on a dielectric interface at the Brewster Angle? Please explain why? (10%)
- (c) Oblique incident from air onto a lossless, nonmagnetic dielectric at a certain incidence angle is observed to result in 80% power transmission when TE polarization is used and in 100% power transmission when TM polarization is tried. What are the index of refraction n of the dielectric and the angle of incidence θ ? (15%)

Problem 4. (20%)

A 2950m-long, lossless telephone line is subjected to a 24V $u(t)$ (step) source having an internal resistance of 100Ω . The per-unit-length inductance and capacitance of the line are $1.15 \mu\text{H/m}$ and 10 pF/m , respectively. The transmission line is terminated into a load resistance of 500Ω .

- (a) What is the lattice diagram (or bounce diagram) for calculating the transient behavior on transmission line? Please briefly describe. (5%)
- (b) Sketch the voltage and current waveforms as a function of time at the midpoint using the lattice diagram. (15%)

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