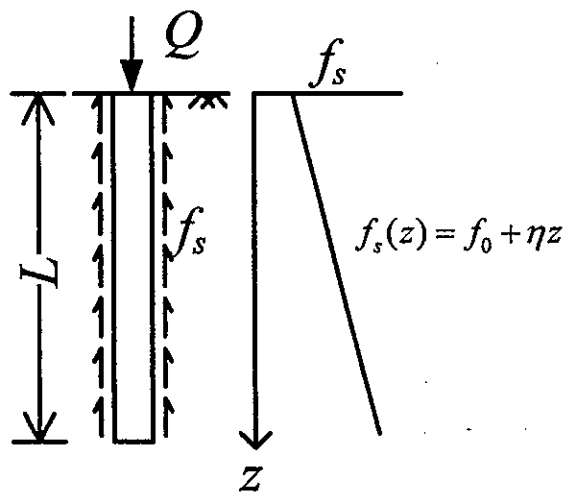


**Problem 1 (25%)**

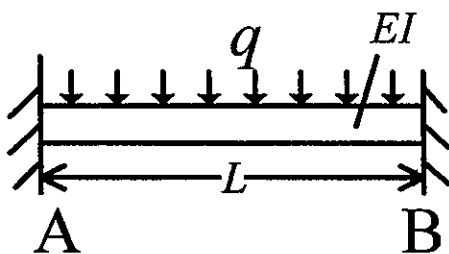
A circular pile is subjected an axial load  $Q$  and skin frictions  $f_s$  as presented in the figure. The pile has a diameter  $D$ , Young's modulus  $E$ , and a length  $L$ . Given that the variation of skin friction per unit area  $f_s(z)$  with depth is  $f_s(z) = f_0 + \eta z$ , derive the pile axial force distribution with depth and the pile deformation.



**Problem 2 (25%)**

A fixed-fixed beam of a flexural rigidity  $EI$  and a length  $L$  is subjected to a surcharge  $q$  as shown in the figure. Use the fourth-order differential beam equation to answer the following questions:

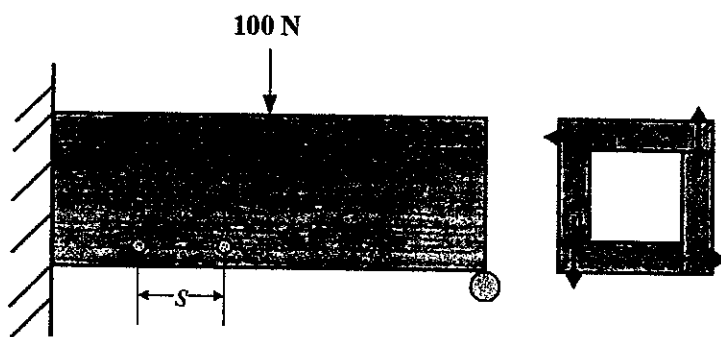
- (i) (10%) Derive the fixed-end moments and shear forces of the beam. (The directions of the moment and shear force have to be noted.)
- (ii) (15%) If end B is subjected to a downward displacement  $\Delta$ , how do the moments and shear forces at ends A and B change due to this dislocation?



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**Problem 3 (25%)**

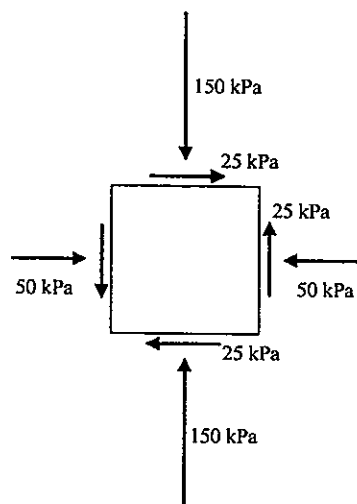
A 1 m long box beam is to be constructed by using four wood boards (1.5 cm × 6.0 cm; elastic modulus = 10 GPa) nailed together as shown in the figure. Assuming that each nail can support a shear force of 25 N, determine the maximum spacing  $s$  of nails so that the beam can support a vertical force of 100 N at the middle of the beam.



**Problem 4 (25%)**

The figure below presents the stresses of a soil element in a sandy stratum subjected to loading. Use Mohr's circle to answer the following questions:

- (i) (10%) Find out the maximum and minimum principal stresses and indicate the planes they act on. (draw a soil element diagram to show them).
- (ii) (15%) If this soil element is at failure, determine the shear strength parameters  $c$  and  $\phi$  of the soil, the location of paired failure planes, and the stresses on the failure planes. (Draw a soil element diagram to show them).



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