

1. A bungee cord that behaves linearly elastically has an unstressed length $L_0 = 760\text{mm}$ and a stiffness $k = 140\text{ N/m}$. The cord is attached to two pegs, distance $b = 380\text{ mm}$ apart, and pulled at its midpoint by a force $P = 80\text{ N}$ (see figure 1). (20%)
- (a) How much strain energy U is stored in the cord?
 - (b) What is the displacement δ_c of the point where the load is applied?
 - (c) Compare the strain energy U with quantity $P\delta_c/2$.
- (Note: The elongation of the cord is not small compared to original length.)

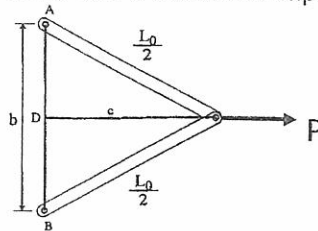


Figure 1

2. A cantilever beam of rectangular cross section (with $b = 25\text{mm}$, height $h = 100\text{mm}$) is loaded by a force P that acts at the midheight of the beam and is inclined at an angle α to the vertical (see figure 2). Two strain gages are placed at point C, which also is at the midheight of the beam. Gage A measures the strain in the horizontal direction and gage B measures the strain at an angle $\beta = 60^\circ$ to the horizontal. The measured strains are $\epsilon_a = 125 \times 10^{-6}$ and $\epsilon_b = -375 \times 10^{-6}$. Determine the force P and the angle α , assuming the material is steel with $E = 200\text{ Gpa}$ and $\nu = 1/3$. (20%)

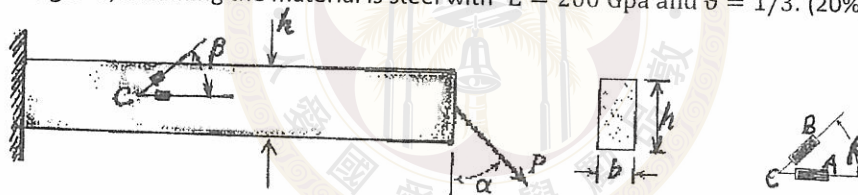


Figure 2

3. (a) A compression member in a bridge truss is fabricated from a wide-flange steel section (see figure 3a). The cross-sectional area $A = 6640\text{ mm}^2$ and the axial load $P = 140\text{ kN}$. (10%) Determine the normal and shear stresses acting on all faces of stress elements located in the web of the beam and oriented at (i) an angle $\theta = 0^\circ$, (ii) an angle $\theta = 22.5^\circ$ and (iii) an angle $\theta = 45^\circ$. In each case, show the stresses on a sketch of a properly oriented element.

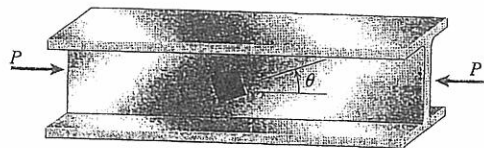


Figure 3a

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3. (b) Two circular shafts (made by the same material) are used to transmit a torque as shown in Fig.3b. If the two shafts have the same cross-sectional area, which one can transmit more torque? Why? (10%)

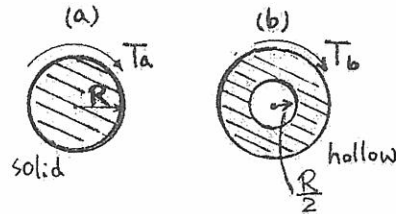


Fig 3b

4. The beam is subjected to the distributed loading shown in Fig. 4. Assume that EI is constant, where E is the Young's modulus and I is the second moment of area of the transverse section with respect to the neutral axis.
- Determine the reactions at A and B. (10%)
 - Find the location and value of the maximum deflection of the beam. (10%)

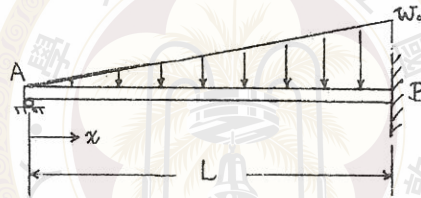


Fig 4

5. A simple beam AB is loaded by two segments of uniform load and two horizontal forces acting at the end of a vertical rigid arm (see Fig. 5a). The cross-section of the beam is shown in Fig. 5b.
- Draw the shear-force and bending-moment diagrams for the beam. (10%)
 - Find the distribution of flexural stress at the location $x = 3m$. Also determine the principal stresses at point A. (10%)

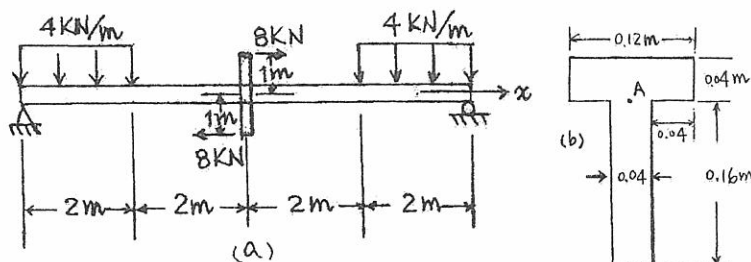


Fig 5

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