

※ 注意：請於試卷上依序作答，並應註明作答之大題及其題號。

一、分析化學試題 (50%)

1. Drugs often absorb strongly in the uv. As an example,  $\epsilon_{254} = 16000$  and  $\epsilon_{267} = 19000$  for tetracycline, while  $\epsilon_{254} = 16000$  and  $\epsilon_{267} = 15000$  for epi-tetracycline, an inactive hydrolysis product. If a mixture exhibits absorbances of 0.402 at 254 nm and 0.432 at 267 nm, what is the concentration of each compound? 12%
2. a. If the transmittance of the compound is measured with an uncertainty,  $\sigma_T$ , derive how this uncertainty is propagated to the measured uncertainty of concentration.  
b. A spectrophotometric analysis was performed with a manual instrument that exhibited an absolute standard deviation of  $\pm 0.003T$  throughout its transmittance scale. Calculate the relative standard deviation in concentration that results from this uncertainty when the analyte solution has an absorbance of 1.000. 12%
3. a. The voltage for the following cell is 0.503 V at room temperature. Find  $K_a$  for the acetic acid.  

$$\text{Pt(s)} \mid \text{H}_2 (1.00 \text{ bar}) \mid \text{CH}_3\text{COOH} (0.050 \text{ M}), \text{CH}_3\text{COONa} (0.0050 \text{ M}) \parallel \text{Cl}^- (1.0 \text{ M}) \mid \text{AgCl(s)} \mid \text{Ag(s)}, \text{ given } E^\circ(\text{AgCl/Ag}) = 0.222 \text{ V}.$$
  
b. Find formation constant for the complex  $\text{Ag}(\text{S}_2\text{O}_3)_2^{3-}$ , given  $E^\circ(\text{Ag}(\text{S}_2\text{O}_3)_2^{3-}/\text{Ag}) = 0.017 \text{ V}$  and  $K_{sp}(\text{AgCl}) = 1.82 \times 10^{-10}$ . 14%
4. An ion having  $m/q=60$  ( $m$ : ion mass;  $q$ : charge) is driven in a time-of-flight mass spectrometer with a flight length 100 cm and an accelerating voltage 3000 V. Calculate (a) the ion speed, and (b) the arrival time of the ion. 12%  
(1 eV =  $1.602 \times 10^{-12}$  erg)

二、物化試題 (50%)

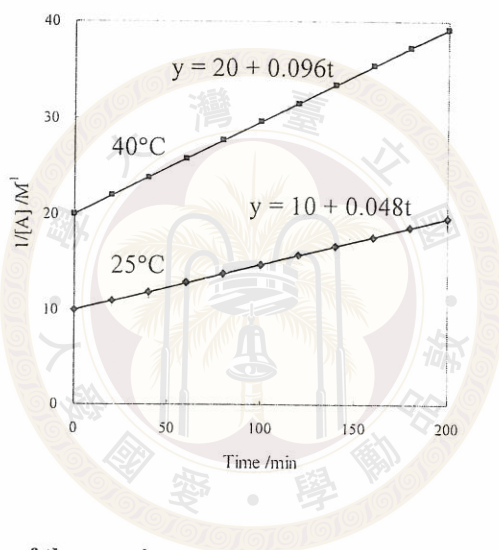
1. For an isothermal reversible expansion of an ideal gas (with constant  $C_v$ ), state whether each of the following is positive, negative or zero:  $q$  (heat),  $w$  (work),  $\Delta U$  ( $U$ : internal energy),  $\Delta H$ ,  $\Delta S$ , and  $\Delta G$ . (no explanation is required) 6%

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2. For an adiabatic reversible compression of 1 mol of an ideal gas (with a molar heat capacity  $C_{vm} = 5R/2$ ) at STP to 2 atm, answer the following questions. 18%

- (A) Give the value of  $\gamma = C_p/C_v$
- (B) Show that  $\left(\frac{\partial P}{\partial T}\right)_S = \frac{C_p}{V}$
- (C) Show that  $P = 3.0 \times 10^{-9} \times T^{3.5}$ .
- (D) Find the final temperature of the process.
- (E) Find the entropy change ( $\Delta S$ ) of the process,
- (F) Find the enthalpy change ( $\Delta H$ ) of the process.
- (G) Find the work done during the process.

3. The plots of  $1/[X]$  vs. time at 25°C and 40°C for the reaction  $2 X \rightarrow \text{products}$  are shown below. ( $R = 8.31 \text{ J}\cdot\text{K}^{-1}\cdot\text{mol}^{-1}$ ) 12%



- (A) Give the rate law of the reaction.
- (B) Find the rate constants of the reaction at these two temperatures.
- (C) Calculate the half-life of the reaction at 40°C.
- (D) Estimate the activation energy (in  $\text{kJ}\cdot\text{mol}^{-1}$ ) of the reaction.

4. Assume an electron ( $m_e = 9.1 \times 10^{-31} \text{ kg}$ ) is confined within 5 nm of a one dimensional particle-in-a-box. Answer the following questions. 14%

- (A) Write the Schrödinger equation for the system.
- (B) Find the ground state energy of the electron. ( $h = 6.625 \times 10^{-34} \text{ J}\cdot\text{s}$ )
- (C) Give four criteria that a trial function must satisfy for use in variation theory.
- (D) Assume the function  $x(l-x)$  is a trial function for the ground state of the 1-D particle-in-a-box with length  $l$ , find the normalization constant for the function.
- (E) Find an expression for the energy of the trial function  $x(l-x)$ .